



Chapter Four

Structural Analysis and Design

4.1 Introduction.

4.2 Design method and requirements.

4.3 Check of minimum thicknesses of structural members.

4.4 Design of topping.

4.5 (Rib 1 or 3 , BF) Calculations.

4.6 (Beam 2, BF) Design of Beam.

4.1 Introduction:

Many structures are built of reinforced concrete: bridges, buildings, retaining walls, tunnels, and others.

Reinforced concrete is logical union of two materials: plain concrete, which possesses high compressive strength but little tensile strength, and steel bars embedded in the concrete, which can provide the needed strength in tension.

Plain concrete is made by mixing cement, fine aggregate, coarse aggregate, water, and frequently admixtures.

Understanding of reinforced concrete behavior is still far from complete, building codes and specifications that give design procedures are continually changing to reflect latest knowledge.

Structural concrete can be classified into:

- Lightweight concrete with unit weight from about 1350 to 1850 kg/m³.
- Normal weight concrete with unit weight from about 1800 to 2400 kg/m³.
- Heavyweight concrete with unit weight from about 3200 to 5600 kg/m³.

4.2 Design method and requirements:

The design strength provided by a member is calculated in accordance with the requirements and assumptions of **ACI_code (318_14)**.

✓ **Strength design method:**

In ultimate strength design method, the service loads are increased by factors to obtain the load at which failure is considered to be occurring.

This load called factored load or factored service load. The structure or structural element is then proportioned such that the strength is reached when factored load is acting.

The computation of this strength takes into account the nonlinear stress-strain behavior of concrete.

The strength design method is expressed by the following,
Strength provided \geq strength required to carry factored loads.

NOTE:

The statically calculation and the key plans dependent on the architectural plans.

✓ Code : ACI 2014

UBC

✓ Material :

Concrete: B350.... ($f_c' = 35 \times 0.8 = 28 \text{ MPa}$) .

Reinforcement steel : The specified yield strength of the reinforcement

{ $f_y = 420 \text{ N/mm}^2 (\text{MPa})$ }

Mild steel : A-36

Connection Type : Weld , Bolts

✓ **Factored loads:**

The factored loads for members in our project are determined by:

$W_u = 1.2 D_L + 1.6 S_L$ ACI-code-318-14(9.2.1).

4.3 Check of minimum thickness of structural member :

TABLE 9.5(a) — MINIMUM THICKNESS OF NONPRESTRESSED BEAMS OR ONE-WAY SLABS UNLESS DEFLECTIONS ARE CALCULATED. (ACI 318M-14)

	Minimum thickness , h			
	Simply supported	One end continuous	Both end continuous	Cantilever
Member	Members not supporting or attached to partitions or other construction likely to be damaged by large deflection			
Solid one way Slabs	L/20	L/24	L/28	L/10
Beams or ribbed one way slabs	L/16	L/18.5	L/21	L/8

Table (4.1): Check of minimum thickness of structural members

For rib :

$$h_{\min} = L/18.5 = 6.13/18.5 = 33.14 \text{ cm}$$

select : 35cm thickness with 27 cm block and 8 topping .

For beam :

$$h_{\min \text{for (one end continuous)}} = L/18.5 = 6.93/18.5 = 37.46 \text{ cm}$$

select $h = (27 + 8) = 35 \text{ cm}$ for rib slab with drop beam $h = 50 \text{ cm}$ (deflection control).

4.4 Design of topping:

✓ **Statically system for topping :**

Consider the topping as strip of (1m) width, and span of mold length with both end fixed in the ribs

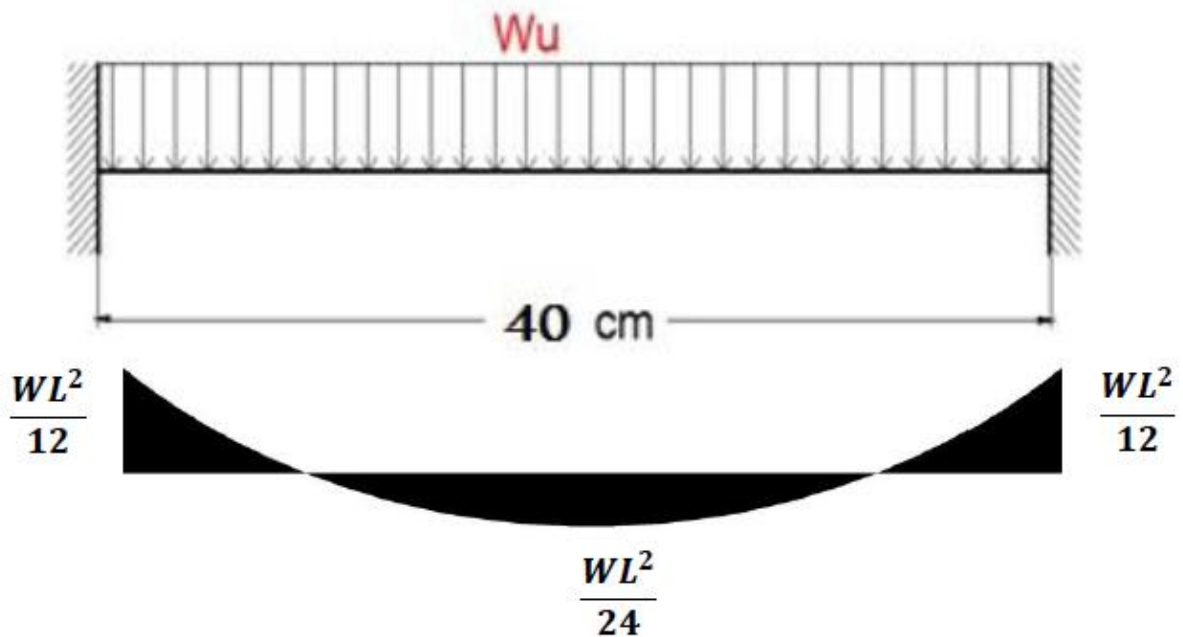


Fig 4.1: topping load and moment diagram.

For the topping , the total dead load to be used in the analysis and design is calculated as follows:

Table (4 – 2) Dead load calculation for topping

No.	Partsof Rib	Quality Density KN/m ³	Calculation
1	Reinforced Concrete Topping	25	$0.08 \times 25 \times 1$
2	Sand	16	$0.07 \times 16 \times 1$
3	Mortar	22	$0.02 \times 22 \times 1$
4	Tile	23	$0.03 \times 23 \times 1$
5	Partition	0	0×1
$\Sigma =$			4.25 KN/m

Nominal total dead load = 4.25 KN/m^2 .
 Nominal total live load = 5 KN/m^2 .

Design of topping for ribbed slab as a plain concrete section :-

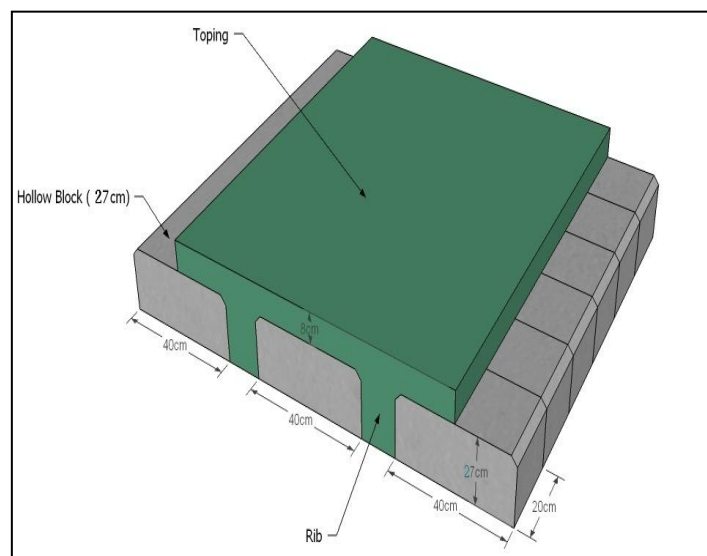


Fig. (4-2) : Topping of one way rib slab

$$q_u = 1.2 \times D + 1.6 \times L$$

13.1 kN/m. (total factored load)

$$\text{Max } M_u = \frac{W_u * l^2}{12} = 0.175 \text{ KN.m}$$

$$\text{Max } V_u = \frac{W_u * l}{2} = 2.62 \text{ KN.m}$$

Design of shear:

Used $f_y = 420 \text{ MPa}$ & $f_c' = 24 \text{ MPa}$

$$\Phi * V_c = 0.75 \times \sqrt{28} \times \frac{1}{6} \times 1000 \times 80 = 52.92 \text{ kN} \gg 2.62 \text{ kN}$$

No shear reinforcement is required.

Design of Moment:

$$\Phi M_n = 0.55 * 0.42 * \sqrt{28} * 1000 * 80^2 / 6 = 1.3 \text{ KN.m}$$

$$\Phi M_n = 1.3 \text{ KN.m} > M_u = 0.175 \text{ KN.m}$$

No structural reinforcement is required.

The strength of plain concrete section > loaded section.

The plain concrete section is safe; however, minimum reinforcement for shrinkage and temperature to control the cracks should be used.

$$\rho = 0.0018 \quad , ACI-318-11$$

$$A_s = \rho * b * h = 0.0018 * 1000 * 80 = 144 \text{ mm}^2.$$

∴ Use $\Phi 8 @ 15 \text{ cm}$

$$A_s = 335.1 \text{ mm}^2 / \text{m} > A_{s_{\min}} = 144 \text{ mm}^2 / \text{m} \quad \text{Ok}$$

4.5) Design Rib : Design of Rib R12

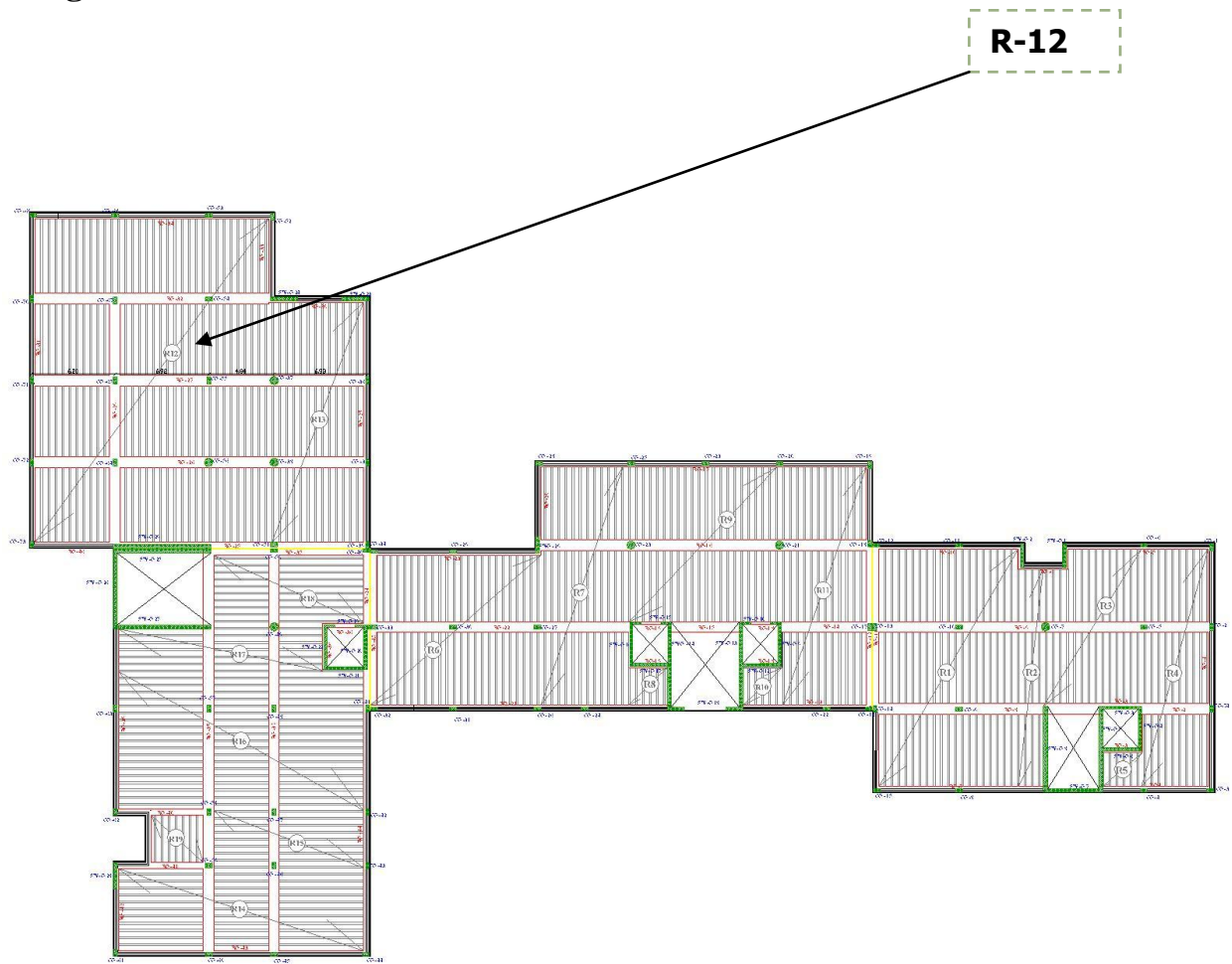


Fig. (4-3) :Ground floor Ribs

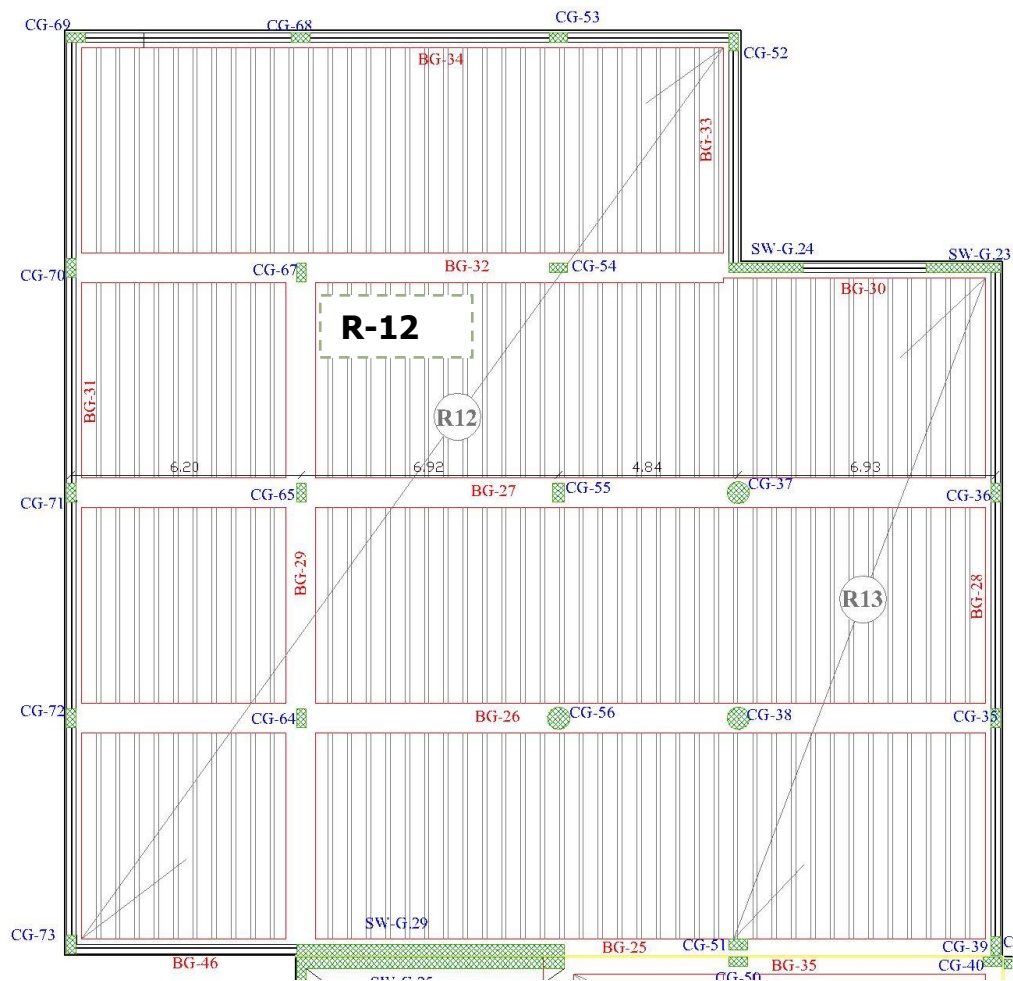


Fig. (4-4) :Rib (12) location in ground floor

For the one-way ribbed slabs, the total dead load to be used in the analysis and design is calculated as follows:

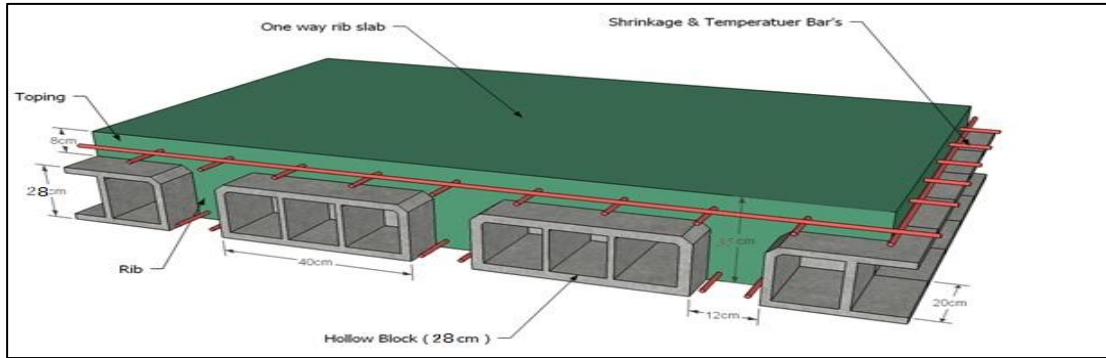


Fig. (4-5) : One way rib slab

Calculation of the total dead load for one way rib slab is shown in the following table:

Table (4 – 3) Calculation of the total dead load for one way rib slab.

N o.	Material	Quality Density KN/m ³	Calculation
1	Topping	25	$0.52 \times 0.08 \times 25 = 1.04$
2	Rib	25	$0.27 \times 0.12 \times 25 = 0.81$
3	Sand	16	$0.52 \times 0.07 \times 16 = 0.5824$
4	Mortar	22	$0.52 \times 0.02 \times 22 = 0.2288$
5	Tile	23	$0.52 \times 0.03 \times 23 = 0.3588$
6	Plaster	22	$0.52 \times 0.02 \times 22 = 0.2288$
7	Block	15	$0.4 \times 0.27 \times 15 = 1.62$
8	Partitions	0.0	0.0
$\Sigma =$			4.87 KN/m

By using **ATIR** program we get the envelope moment and shear force diagram as the follows:-

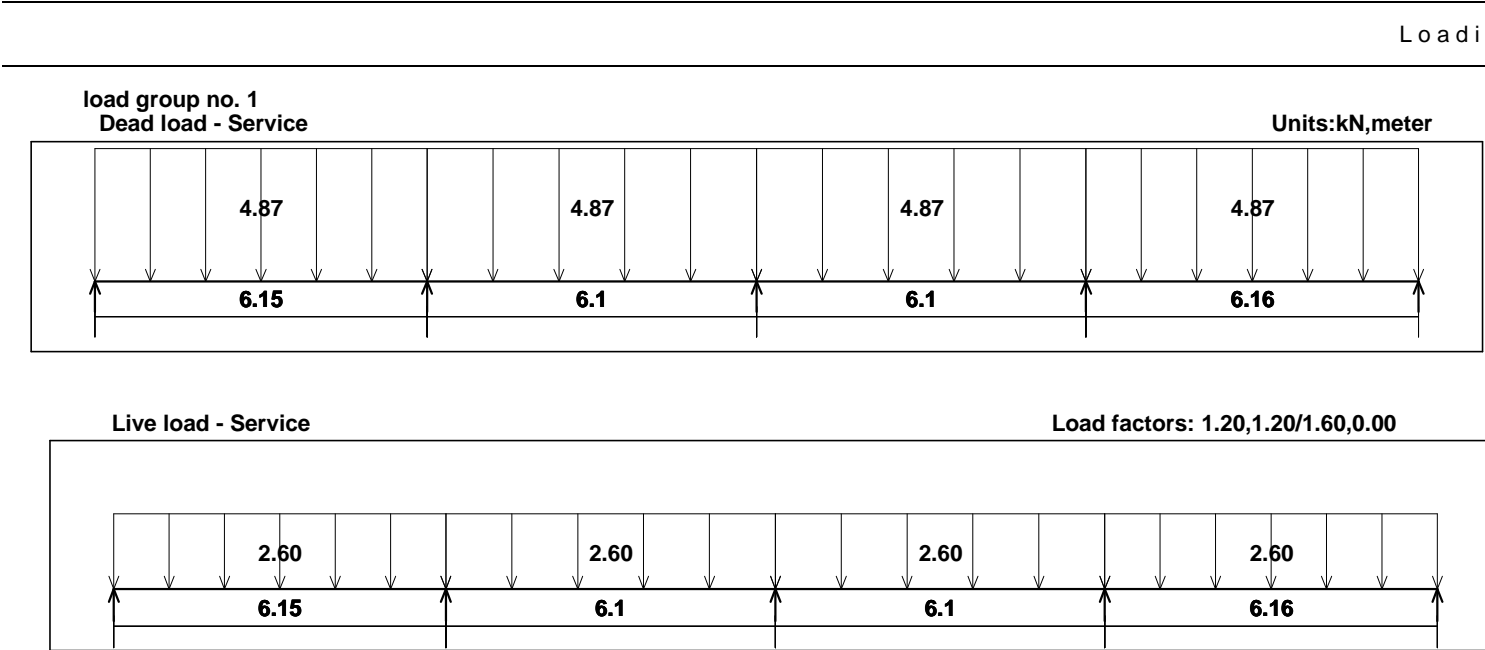
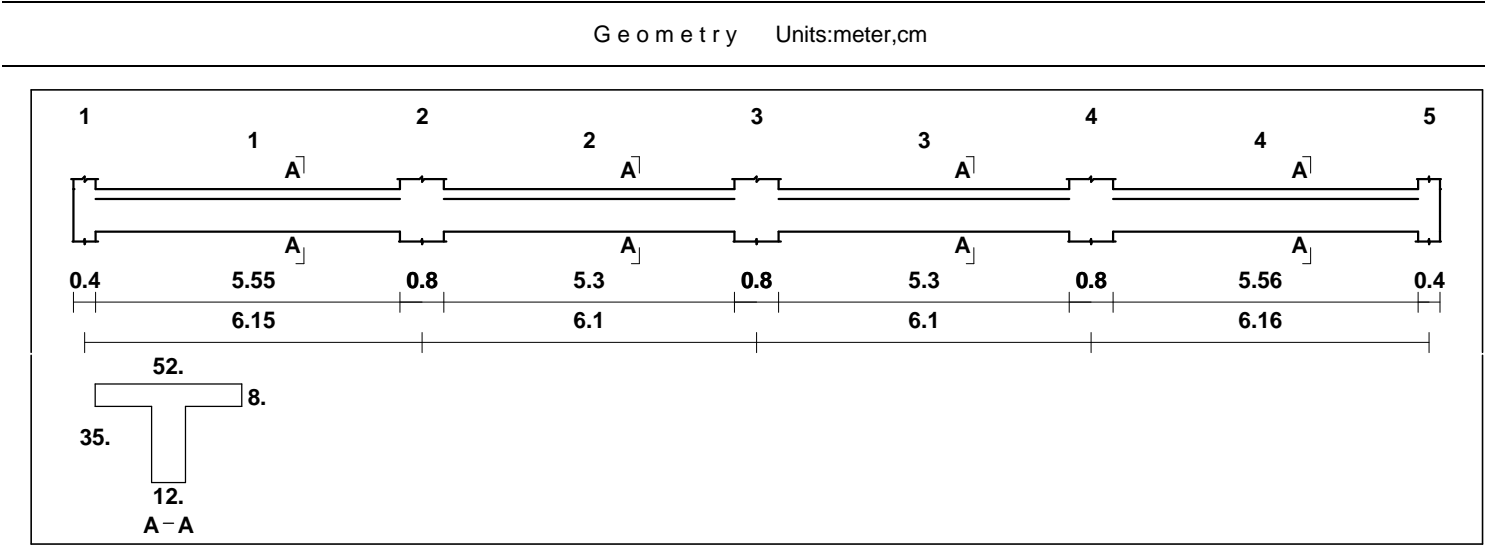
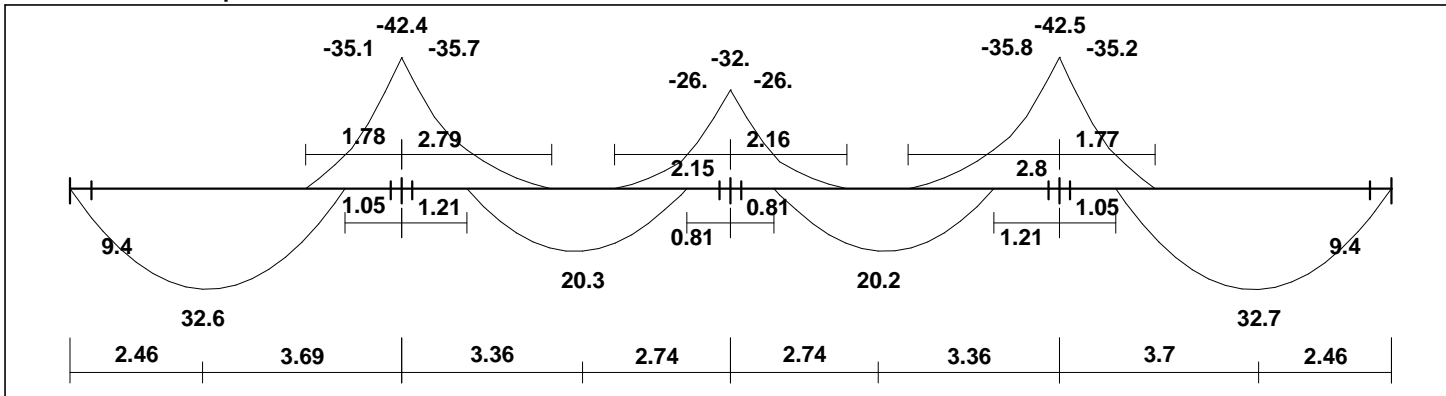


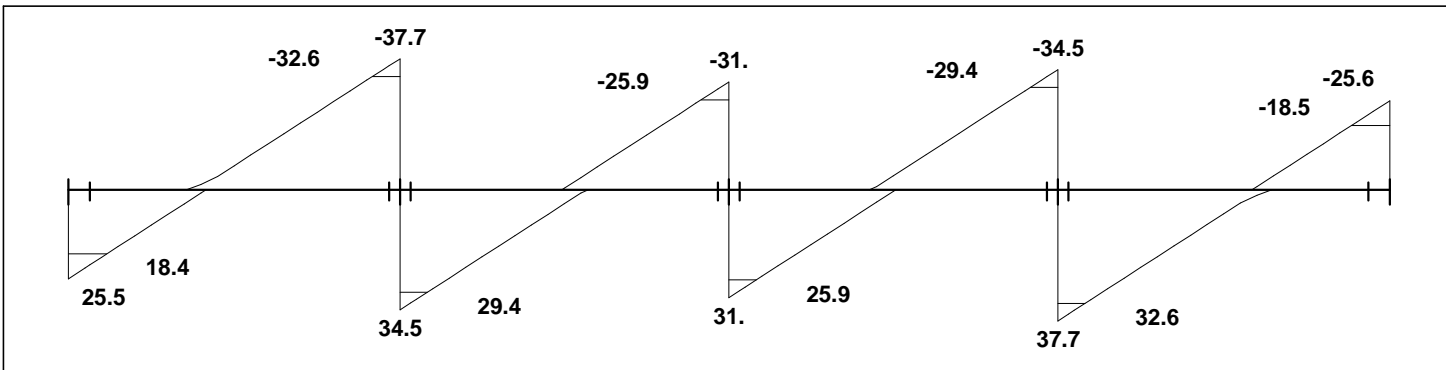
Figure (4.7) Loading of rib R12(KN/m).

Moment/Shear Envelope (Factored) Units:kN,meter

Moments: spans 1 to 4



Shear



Reactions

Factored					
DeadR	14.14	40.97	32.95	41.01	14.16
LiveR	11.41	31.2	29.02	31.23	11.42
Max R	25.55	72.17	61.97	72.24	25.59
Min R	12.79	52.74	41.9	52.77	12.82
Service					
DeadR	11.78	34.14	27.46	34.18	11.8
LiveR	7.13	19.5	18.13	19.52	7.14
Max R	18.91	53.64	45.6	53.69	18.94
Min R	10.94	41.5	33.05	41.53	10.97

Figure (4.8) Moment and Shear Envelop for rib R12

- **Design of shear for rib R12**

Categories for shear design:

$$V_u = 32.6 \text{ KN}$$

Use $\Phi 8$ with two legs

$$d = 350 - 20 - 8 - 7 = 315$$

1. Region I :

$$1.1\Phi V_c \geq V_u$$

$$1.1\Phi V_c = 1.1\Phi \frac{\sqrt{f_c'}}{6} \times b_w \times d$$

$$1.1\Phi V_c = 1.1 \times 0.75 \times \frac{\sqrt{28}}{6} \times 120 \times 315 = 27.5 \text{ KN} < V_u = 32.6 \text{ KN}$$

$$\Phi V_{s \min} = \Phi \times \frac{\sqrt{f_c'}}{16} \times b_w \times d$$

$$\Phi V_{s \min} = 0.75 \times \frac{\sqrt{28}}{16} \times 120 \times 315 = 9.38 \text{ KN}$$

$$\Phi V_{s \min} = \Phi \left(\frac{1}{3} \right) \times b_w \times d$$

$$\Phi V_{s \min} = 0.75 \left(\frac{1}{3} \right) \times 120 \times 315 = 9.45 \text{ KN}$$

$$\Phi V_c + \Phi V_{s \min} = 25 + 9.45 = 34.45 \text{ KN}$$

$$27.5 \text{ KN} < 32.6 \text{ KN} \leq 34.45 \text{ KN}$$

Case III minimum Shear reinforcement required .So,

Use $\Phi 8, 2$ leg

$$A_v = 100.53 \text{ mm}^2.$$

$$V_s = \frac{v_u}{\phi} - v_c = \frac{32.6}{0.75} - 33.33 = 10.14 \text{ KN}$$

$$S_{req} = \frac{A_v f_{yt} d}{v_s} = \frac{100.53 * 420 * 315}{10.14 * 1000} = 1311.65 \text{ mm}$$

$$S_{req} \leq S_{max}$$

$$S_{max} \leq \frac{d}{2} \text{ or } S_{max} \leq 600 \text{ mm}$$

$$\frac{d}{2} = \frac{315}{2} = 158 \text{ mm (control)}$$

Use $\Phi 8$, @ 15 cm (2Legs).

• **Design of Positive Moment:**

Effective Flange width (b_E) , ACI-318-14

b_E For T- section is the smallest of the following:

$$b_E = (2200) / 4 = 550 \text{ mm}$$

$$b_E = 120 + 16 (80) = 1400 \text{ mm}$$

$$b_E = 520 \text{ mm} \dots \dots \dots \text{ control}$$

» Use M_u max positive for span 1 = 32.6 kN.m

» Determine whether the rib will act as rectangular or T – section:

For $h_f = 0.08 \text{ m}$

~ Assume bar diameter $\Phi 14$ for main positive reinforcement.

$$d = 350 - 20 - 8 - 7 = 315 \text{ mm}$$

$$\Phi * M_n = 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2)$$

$$= 0.9 * 0.85 * 28 * 0.52 * 0.08 * (0.315 - 0.08/2) = 245 \text{ KN.m}$$

$$\Phi * M_n = 245 \text{ KN.m} >> M_u = 32.6 \text{ KN.m}$$

The section will be designed as a rectangular section with $b_E = 520 \text{ mm}$

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) > A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(315) = 119.1 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \sim \underline{\text{control}}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$Kn = \frac{Mu}{\Phi b d^2} = \frac{32.6 * 10^6}{(0.9)(520)(315)^2} = 0.70 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * kn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.7}{420}} \right) = 0.00169$$

$$A_s = 0.00169(520)(315) = 276.82 \text{ mm}^2 > A_s \min = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 276.82/154 = 1.798 \quad * \text{ Note } A_{\Phi 14} = 154 \text{ mm}^2$$

Select bottom bars 2Φ14

$$\text{Total } A_s (\text{provide}) = 308 \text{ mm}^2 > 276.82 \text{ mm}^2$$

* Check Strain for the magnitude of under strength factor Φ:

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$308 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 10.45 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{10.45}{0.85} = 12.29 \text{ mm}$$

$$\epsilon_s = \frac{315 - 12.29}{12.29} \times 0.003 = 0.0739$$

$$\epsilon_s = 0.0739 > 0.005$$

Ok.....

» Use M_u max positive for span 2 = 20.3 kN.m

» Determine whether the rib will act as rectangular or T – section:

For hf = 0.08 m

~ Assume bar diameter $\Phi 14$ for main positive reinforcement.

$$d = 350 - 20 - 8 - 7 = 315 \text{ mm}$$

$$\Phi * M_n = 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2)$$

$$= 0.9 * 0.85 * 28 * 0.52 * 0.08 * (0.315 - 0.08/2) = 245 \text{ KN.m}$$

$$\Phi * M_n = 245 \text{ KN.m} \gg M_u = 20.3 \text{ KN.m}$$

The section will be designed as a rectangular section with $b_E = 520 \text{ mm}$

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \geq A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(315) = 119.1 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \sim \text{control}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$Kn = \frac{Mu}{\Phi b d^2} = \frac{20.3 * 10^6}{(0.9)(520)(315)^2} = 0.44 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * kn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.44}{420}} \right) = 0.00106$$

$$A_s = 0.00106(520)(315) = 173.63 \text{ mm}^2 > A_s \min = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 173.63/113 = 1.53 \quad * \text{ Note } A_{\Phi 12} = 113 \text{ mm}^2$$

Select bottom bars 2 $\Phi 12$

$$\text{Total } A_{s \text{ (provide)}} = 226.19 \text{ mm}^2 > 173.63 \text{ mm}^2$$

* Check Strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$226.19 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 7.68 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{7.68}{0.85} = 9 \text{ mm}$$

$$\varepsilon_s = \frac{315 - 9}{9} \times 0.003 = 0.102$$

$$\varepsilon_s = 0.102 > 0.005 \quad \square$$

Ok.....

»Use M_u max positive for span 3 = 20.2kN.m = "span 2 M_u max=20.3kN.m"

» Determine whether the rib will act as rectangular or T – section:

For $h_f = 0.08$ m

~ Assume bar diameter $\Phi 14$ for main positive reinforcement.

$$d = 350 - 20 - 8 - 7 = 315 \text{ mm}$$

$$\begin{aligned} \Phi * M_n &= 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2) \\ &= 0.9 * 0.85 * 28 * 0.52 * 0.08 * (0.315 - 0.08/2) = 245 \text{ KN.m} \end{aligned}$$

$$\Phi * M_n = 245 \text{ KN.m} >> M_u = 20.3 \text{ KN.m}$$

The section will be designed as a rectangular section with $b_E = 520$ mm

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) > A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(315) = 119.1 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \sim \underline{\text{control}}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$Kn = \frac{Mu}{\Phi b d^2} = \frac{20.3 * 10^6}{(0.9)(520)(315)^2} = 0.44 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * kn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.44}{420}} \right) = 0.00106$$

$$A_s = 0.00106(520)(315) = 173.63 \text{ mm}^2 > A_s \min = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 173.63 / 113 = 1.53 \quad * \text{ Note } A_{\Phi 12} = 113 \text{ mm}^2$$

Select bottom bars 2 $\Phi 12$

$$\text{Total } A_s (\text{provide}) = 226.19 \text{ mm}^2 > 173.63 \text{ mm}^2$$

* Check Strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$226.19 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 7.68 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{7.68}{0.85} = 9 \text{ mm}$$

$$\varepsilon_s = \frac{315 - 9}{9} \times 0.003 = 0.102$$

$$\varepsilon_s = 0.102 > 0.005 \quad ?$$

Ok.....

» Use M_u max positive for span 4 = 32.7 kN.m = "span 1 M_u max = 32.6 kN.m "

» Determine whether the rib will act as rectangular or T – section:

For $h_f = 0.08 \text{ m}$

~ Assume bar diameter $\Phi 14$ for main positive reinforcement.

$$d = 350 - 20 - 8 - 7 = 315 \text{ mm}$$

$$\Phi * M_n = 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2)$$

$$= 0.9 * 0.85 * 28 * 0.52 * 0.08 * (0.315 - 0.08/2) = 245 \text{ kN.m}$$

$$\Phi * M_n = 245 \text{ kN.m} >> M_u = 32.6 \text{ kN.m}$$

The section will be designed as a rectangular section with $b_E = 520 \text{ mm}$

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \geq A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(315) = 119.1 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \sim \underline{\text{control}}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$Kn = \frac{Mu}{\Phi b d^2} = \frac{32.6 * 10^6}{(0.9)(520)(315)^2} = 0.70 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * kn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.7}{420}} \right) = 0.00169$$

$$A_s = 0.00169(520)(315) = 276.82 \text{ mm}^2 > A_{s \text{ min}} = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 276.82/154 = 1.798 \quad * \text{ Note } A_{\Phi 14} = 154 \text{ mm}^2$$

Select bottom bars 2Φ14

$$\text{Total } A_{s \text{ (provide)}} = 308 \text{ mm}^2 > 276.82 \text{ mm}^2$$

* Check Strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$308 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 10.45 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{10.45}{0.85} = 12.29 \text{ mm}$$

$$\epsilon_s = \frac{315 - 12.29}{12.29} \times 0.003 = 0.0739$$

$$\epsilon_s = 0.0739 > 0.005$$

Ok.....

- **Design of Max Negative Moment for (Rib):**

»The maximum negative moment from spans with support (2) = "support(4)" is

$$M_u = - 35.8 \text{ kN.m}$$

$$M_n = 35.8 / 0.9 = 39.78 \text{ kN.m}$$

~ Assume bar diameter $\Phi 16$ for main negative reinforcement.

$$d = 350 - 20 - 8 - 8 = 314 \text{ mm}$$

$$\Phi * M_n = 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2)$$

$$= 0.9 * 0.85 * 28 * 0.52 * 0.27 * (0.314 - 0.27/2) = 538.32 \text{ KN.m}$$

$$\Phi * M_n = 538.32 \text{ KN.m} \gg M_u = 35.8 \text{ KN.m}$$

The section will be designed as a rectangular section with $b_E = 520 \text{ mm}$

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \geq A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(314) = 118.7 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(314) = 125.6 \text{ mm}^2 \sim \text{control}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$K_n = \frac{M_u}{\Phi b d^2} = \frac{35.8 * 10^6}{(0.9)(520)(314)^2} = 0.78 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * k_n}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.78}{420}} \right) = 0.00189$$

$$A_s = 0.00189(520)(314) = 308.6 \text{ mm}^2 > A_s \min = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 308.6/201.1 = 1.53 \quad * \text{ Note } A_{\Phi 16} = 201.1 \text{ mm}^2$$

Select top bars 2 $\Phi 16$

$$\text{Total } A_s (\text{provide}) = 402.12 \text{ mm}^2 > 308.6 \text{ mm}^2$$

* Check Strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$402.12 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 13.65 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{13.65}{0.85} = 16.06 \text{ mm}$$

$$\varepsilon_s = \frac{314 - 16.06}{16.06} \times 0.003 = 0.0557$$

$$\varepsilon_s = 0.0557 > 0.005 \quad \square$$

Ok.....

»The maximum negative moment from spans with support (3) is

Mu = 26 kN.m

$$M_n = 26 / 0.9 = 28.89 \text{ kN.m}$$

~ Assume bar diameter $\Phi 14$ for main negative reinforcement.

$$d = 350 - 20 - 8 - 7 = 315 \text{ mm}$$

$$\Phi * M_n = 0.9 * 0.85 * f_c' * b * h_f * (d - h_f/2)$$

$$= 0.9 * 0.85 * 28 * 0.52 * 0.27 * (0.315 - 0.27/2) = 541.33 \text{ KN.m}$$

$$\Phi * M_n = 541.33 \text{ KN.m} \gg M_u = 26 \text{ KN.m}$$

The section will be designed as a rectangular section with $b_E = 520 \text{ mm}$

$$A_s \min = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \geq A_s \min = \frac{1.4}{(f_y)} (b_w)(d) \text{ ACI-318 -14}$$

$$A_s \min = \frac{\sqrt{28}}{4(420)} (120)(315) = 119.1 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \sim \underline{\text{control}}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85(28)} = 17.65$$

$$Kn = \frac{Mu}{\Phi b d^2} = \frac{26 * 10^6}{(0.9)(520)(315)^2} = 0.56 \text{ Mpa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * m * kn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.56}{420}} \right) = 0.00135$$

$$A_s = 0.00135(520)(315) = 221.13 \text{ mm}^2 > A_s \min = 126 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 221.13 / 154 = 1.44 \quad * \text{ Note } A_{\Phi 14} = 154 \text{ mm}^2$$

Select top bars 2Φ14

Total A_s (provide) = $308 \text{ mm}^2 > 126 \text{ mm}^2$

* Check Strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$308 \times 420 = 0.85 \times 28 \times 520 \times a$$

$$a = 10.45 \text{ mm}$$

$$x = \frac{a}{0.85} = \frac{10.45}{0.85} = 12.29 \text{ mm}$$

$$\epsilon_s = \frac{315 - 12.29}{12.29} \times 0.003 = 0.0739$$

$$\epsilon_s = 0.0739 > 0.005$$

?

Ok.....

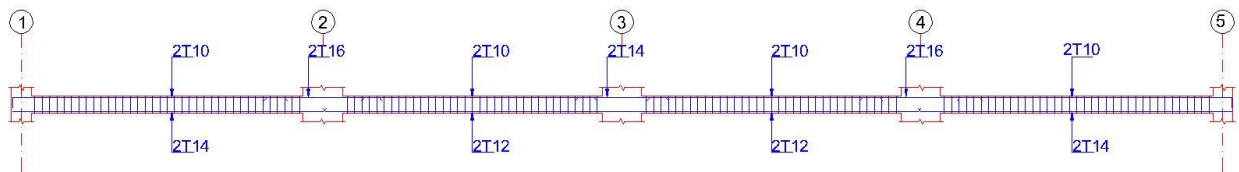
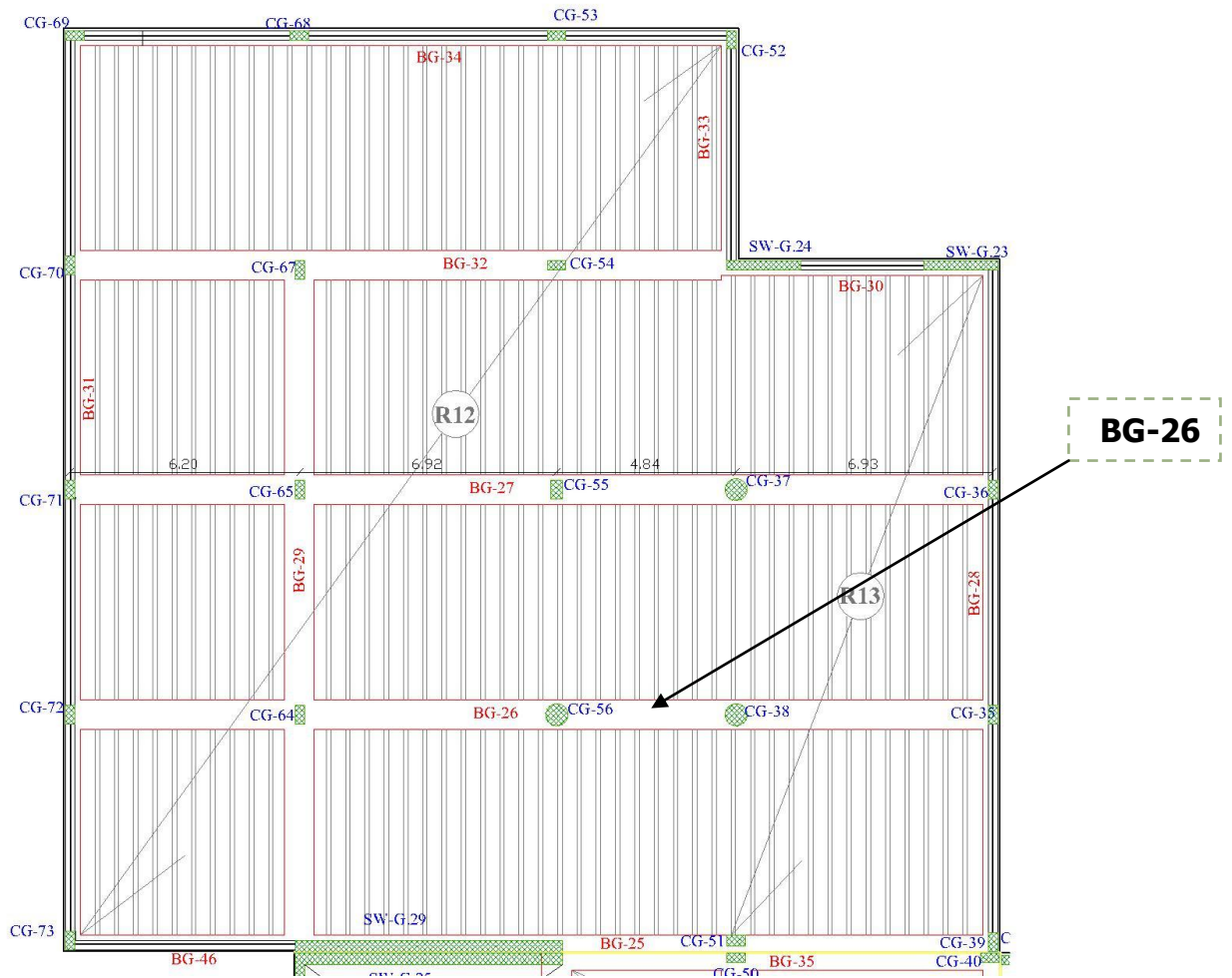


Figure 9 beam detailing

Design of Beam BG-26



Figure(4.10)Beam location in ground floor slab

Load calculations for Beam:

The distributed Dead and Live loads acting upon the Beam **BG-26** can be defined from the support reactions of the rib **R12 AND R13**.

Reactions					
Factored					
DeadR	14.14	40.97	32.95	41.01	14.16
LiveR	11.41	31.2	29.02	31.23	11.42
Max R	25.55	72.17	61.97	72.24	25.59
Min R	12.79	52.74	41.9	52.77	12.82
Service					
DeadR	11.78	34.14	27.46	34.18	11.8
LiveR	7.13	19.5	18.13	19.52	7.14
Max R	18.91	53.64	45.6	53.69	18.94
Min R	10.94	41.5	33.05	41.53	10.97

Figure (4.11) Reaction of rib R12

- The support reaction (service) from Dead loads of Rib (R12) upon beam (BG-26) is **(34.14KN)**. The distributed Dead load from Rib (R12) on Beam(BG-26):

$$DL_{from Rib} = \frac{34.14}{0.52} = 65.65 \text{ KN/m}$$

- The support reaction (service) from Live loads of Rib (R12) upon beam (BG-26) is **(19.52KN)**. The distributed Live load from Rib (RG12) on Beam (BG-26):

$$LL_{from Rib} = \frac{19.52}{0.52} = 37.5 \text{ KN/m}$$

By using **ATIR** program we get the envelope moment and shear diagram as the follows:-

Geometry Units: meter, cm

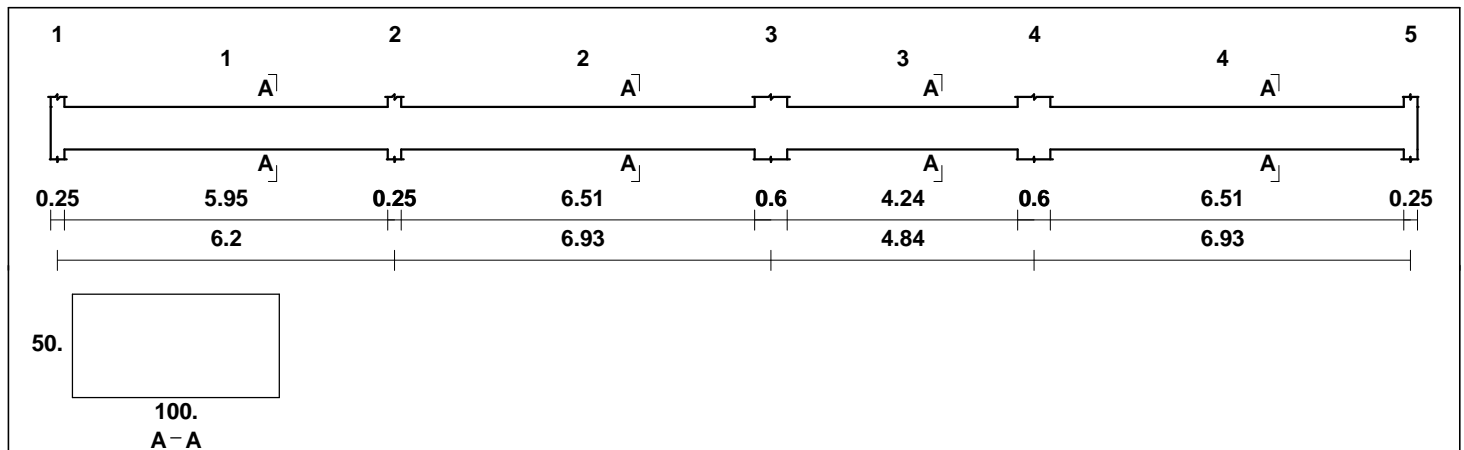


Figure (4.12) Geometry of Beam BG-26

Loading

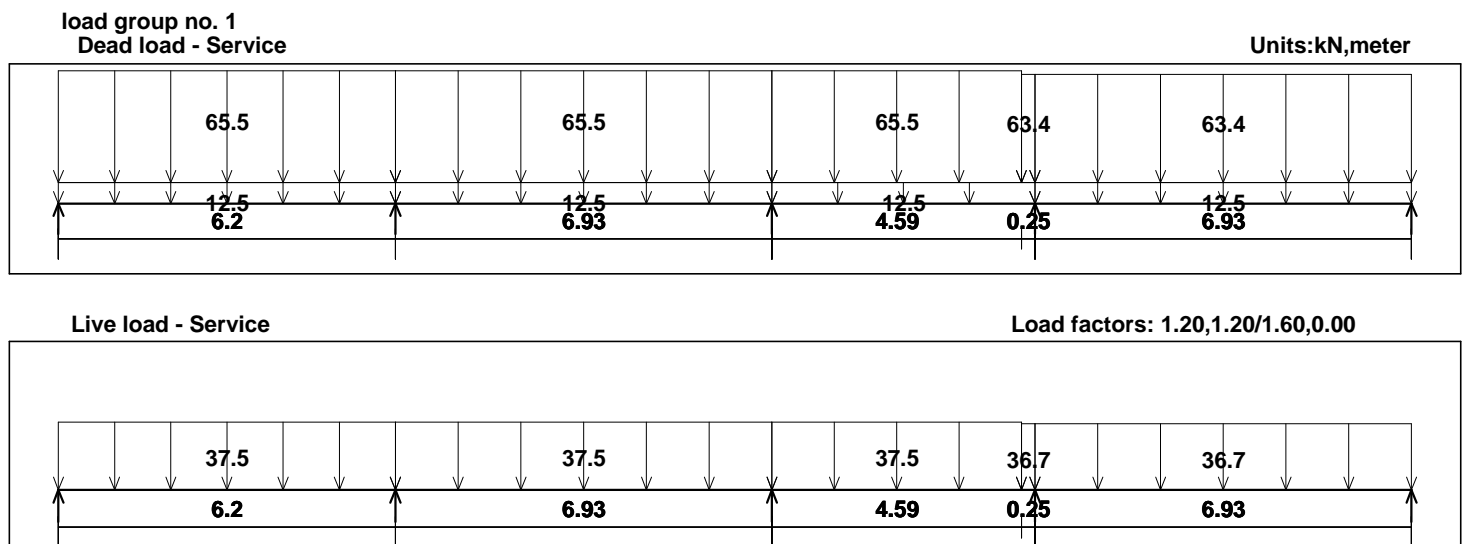
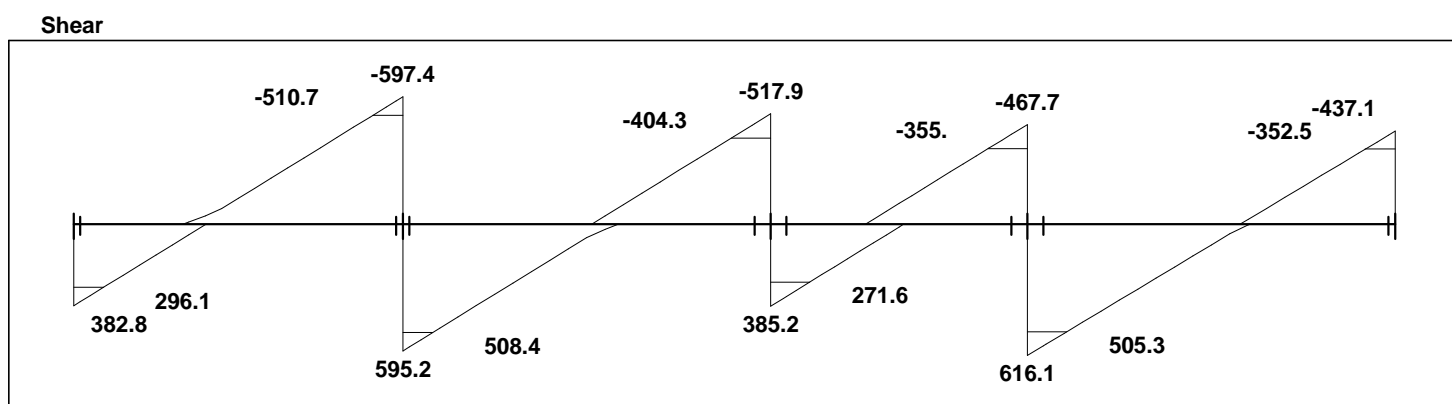
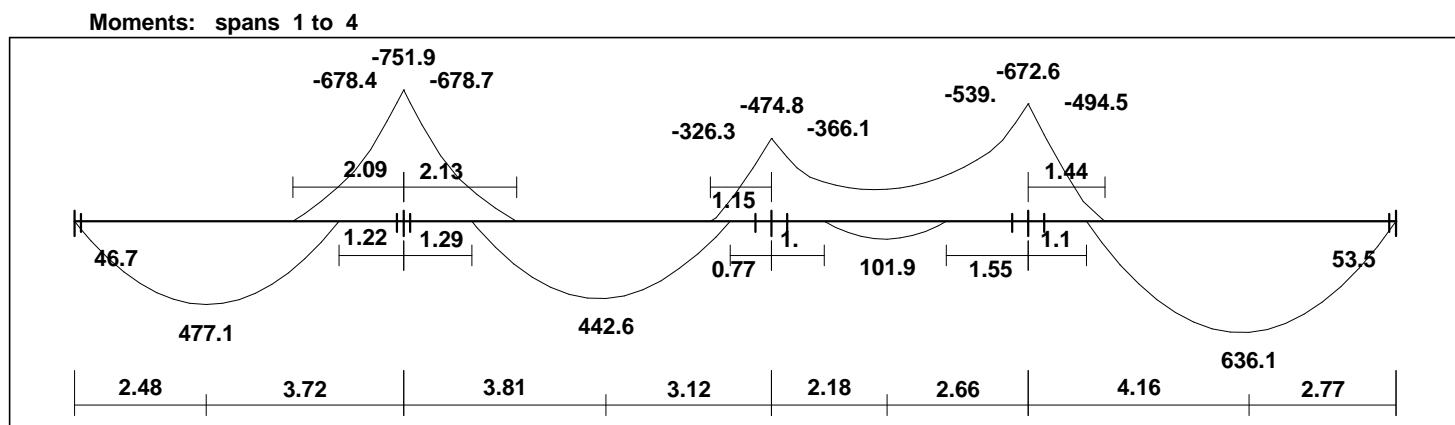


Figure (4.13) Loading of Beam BG-26 (KN/m).

Moment/Shear Envelope (Factored) Units: kN, meter



Reactions

Factored					
DeadR	217.96	717.78	487.77	629.27	259.77
LiveR	164.88	474.85	415.41	454.57	177.34
Max R	382.84	1192.63	903.18	1083.84	437.11
Min R	192.78	929.2	543.08	731.88	249.93
Service					
DeadR	181.63	598.15	406.48	524.39	216.47
LiveR	103.05	296.78	259.63	284.1	110.84
Max R	284.68	894.93	666.11	808.5	327.31
Min R	165.9	730.29	441.04	588.52	210.32

Figure (4.14) Moment and Shear envelop for Beam BG-26

Assume bar diameter $\Phi 25$ for main reinforcement.

Selected drop beam

$$b_w = 80\text{cm}, h = 50\text{cm}$$

$$d = 500 - 40 - 12 - \frac{25}{2} = 435.5\text{mm}$$

- **Design of shear for Beam :**

ACI – 318 – Categories for shear design:

$$V_{u \text{ critical}} = 510 \text{ KN}$$

$$V_c = \frac{1}{6} \sqrt{f'c} b_w d$$

$$V_c = \frac{1}{6} \sqrt{28} * 1000 * 435.5$$

$$V_c = 384.1 \text{ KN.}$$

$$\Phi V_c = 0.75 * 384.1 = 288.1 \text{ KN}$$

$$v_{s,min} = \frac{1}{16} \sqrt{f'c} b_w d$$

$$v_{s,min} = \frac{1}{16} \sqrt{28} * 1000 * 435.5$$

$$v_{s,min} = 144 \text{ kn}$$

$$v_{s,min} = \frac{1}{3} b_w d$$

$$v_{s,min} = \frac{1}{3} * 1000 * 435.5$$

$$v_{s,min} = 145.2 \text{ KN}$$

Case III minimum Shear reinforcement required .So,

$$\Phi(v_c + v_{s,min}) < v_u \leq 3 \Phi * v_c$$

$$0.75(384.1 + 145) = 396.83 < 510 < 3 * 0.75 * 384.1 = 864.23$$

So, shear reinforcement are required.

Use 4 leg Φ 12.

$$A_v = 452.4 \text{ mm}^2.$$

$$V_s = V_u - V_c = \frac{510}{0.75} - 384.1 = 295.9 \text{ KN}$$

$$S = \frac{A_v f_{yt} d}{v_s} = \frac{452.4 * 420 * 435.5}{384.1 * 1000} = 215.43 \text{ mm}$$

$$s_{max} \leq \frac{d}{2} \text{ or } s_{max} \leq 600 \text{ mm}$$

$$S_{max} = \frac{d}{2} = \frac{435.5}{2} = 217.75 \text{ mm}$$

Select 4 leg $\Phi 12$, @ 150 mm (2 Legs)

- Design of Beam of negative moment :

➤ **Mu = -678.7 KN.m at support (2).**

$$M_n = M_u / 0.9$$

$$= 678.7 / 0.9 = 754.11 \text{ KN.m}$$

~ Assume bar diameter $\Phi 25$ for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 \times f_c'} = \frac{420}{0.85 \times 28} = 17.65$$

$$K_n = \frac{M_n}{bd^2} = \frac{678.7 \times 10^6}{(0.9)(1000)(435.5)^2} = 3.98 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2mk_n}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 \times 17.65 \times 3.98}{420}} \right) = 0.0104$$

$$A_s = 0.0104 (1000) (435.5) = 4529.2 \text{ mm}^2 > A_s \text{ min} = 1451.67 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 4529.2 / 491 = 9.22 \quad * \text{ Note } A_{\Phi 25} = 491 \text{ mm}^2$$

Select bar 10 $\Phi 25$

$$\text{Total } A_{s \text{ (provide)}} = 4910 \text{ mm}^2 > 4529.2 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$4910 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 86.65 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{86.65}{0.85} = 101.94 \text{ mm}$$

$$\varepsilon_s = \frac{435.5 - 101.94}{101.94} \times 0.003 = 0.0098$$

$$\varepsilon_s = 0.0098 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 10 \times 25}{9} = 71.78 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

➤ **Mu = -366.1 KN.m at support (3).**

$$\begin{aligned} M_n &= M_u / 0.9 \\ &= 366.1 / 0.9 = 406.78 \text{ KN.m} \end{aligned}$$

~ Assume bar diameter $\Phi 25$ for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 * f_c'} = \frac{420}{0.85 * 28} = 17.65$$

$$K_n = \frac{M_n}{b d^2} = \frac{366.1 * 10^6}{(0.9)(1000)(435.5)^2} = 2.14 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 m k_n}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 2.14}{420}} \right) = 0.00535$$

$$A_s = 0.00535 (1000) (435.5) = 2330 \text{ mm}^2 > A_s \text{ min} = 1451 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 2330 / 491 = 4.75 \quad * \text{ Note } A_{\Phi 25} = 491 \text{ mm}^2$$

Select bar 5 $\Phi 25$

$$\text{Total } A_s (\text{provide}) = 2455 \text{ mm}^2 > 2330 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$2455 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 43.32 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{43.32}{0.85} = 50.96 \text{ mm}$$

$$\varepsilon_s = \frac{435.5 - 50.96}{50.96} \times 0.003 = 0.022$$

$$\varepsilon_s = 0.022 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 5 \times 25}{4} = 192.75 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

➤ **Mu = -539 KN.m at support (4).**

$$M_n = M_u / 0.9$$

$$= 539 / 0.9 = 598.89 \text{ KN.m}$$

~Assume bar diameter $\Phi 25$ for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 * f_c'} = \frac{420}{0.85 * 28} = 17.65$$

$$K_n = \frac{M_n}{b d^2} = \frac{539 * 10^6}{(0.9)(1000)(435.5)^2} = 3.16 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 m k_n}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 3.16}{420}} \right) = 0.0081$$

$$A_s = 0.0081 (1000) (435.5) = 3527.6 \text{ mm}^2 > A_s \text{ min} = 1451 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 3527.6 / 491 = 7.18$$

$$* \text{ Note } A_{\Phi 25} = 491 \text{ mm}^2$$

Select bar 8 $\Phi 25$

$$\text{Total } A_{s \text{ (provide)}} = 3928 \text{ mm}^2 > 3527.6 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$3928 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 69.32 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{69.32}{0.85} = 81.55 \text{ mm}$$

$$\varepsilon_s = \frac{435.5 - 81.55}{81.55} \times 0.003 = 0.013$$

$$\varepsilon_s = 0.013 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 8 \times 25}{7} = 99.43 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

• Design of positive moment :

***Take Mu = 477.1 kN.m at span (1&2).**

~ Assume bar diameter $\Phi 25$ for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 \times f_c'} = \frac{420}{0.85 \times 28} = 17.65$$

$$Kn = \frac{Mn}{bd^2} = \frac{477.1 \times 10^6}{(0.9)(1000)(435.5)^2} = 2.8 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2mn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 \times 17.65 \times 2.8}{420}} \right) = 0.0071$$

$$A_s = 0.0071 (1000) (435.5) = 3092.1 \text{ mm}^2 > A_s \text{ min} = 1451.67 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 3092.1 / 491 = 6.3$$

$$* \text{ Note } A_{\Phi 25} = 491 \text{ mm}^2$$

Select bar 7 Φ 25

$$\text{Total } A_s (\text{provide}) = 3437 \text{ mm}^2 > 3092.1 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$3437 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 60.65 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{60.65}{0.85} = 71.35 \text{ mm}$$

$$\epsilon_s = \frac{435.5 - 71.35}{71.35} \times 0.003 = 0.015$$

$$\epsilon_s = 0.015 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 7 \times 25}{6} = 120.16 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

***Take Mu = 102 KN.m at span (3).**

~ Assume bar diameter Φ25 for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 \times f_c'} = \frac{420}{0.85 \times 28} = 17.65$$

$$Kn = \frac{Mn}{bd^2} = \frac{102 \times 10^6}{(0.9)(1000)(435.5)^2} = 0.6 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2mkn}{f_y}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 \times 17.65 \times 0.6}{420}} \right) = 0.00145$$

$$A_s = 0.00145 (1000) (435.5) = 631.5 \text{ mm}^2 < A_s \text{ min} = 1451.67 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 1451/314 = 2.96$$

$$* \text{ Note } A_{\Phi 25} = 314 \text{ mm}^2$$

Select bar 5 Φ 20

$$\text{Total } A_s (\text{provide}) = 1570 \text{ mm}^2 > 1451.67 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times f_y = 0.85 \times f_c' \times b \times a$$

$$1570 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 27.71 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{27.71}{0.85} = 32.6 \text{ mm}$$

$$\epsilon_s = \frac{435.5 - 32.6}{32.6} \times 0.003 = 0.037$$

$$\epsilon_s = 0.037 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 5 \times 20}{4} = 199 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

***Take Mu = 636.1 kN.m at span (4).**

~ Assume bar diameter $\Phi 25$ for main negative reinforcement.

$$d = 500 - 40 - 12 - 12.5 = 435.5 \text{ mm}$$

$$m = \frac{f_y}{0.85 \times f_c'} = \frac{420}{0.85 \times 28} = 17.65$$

$$Kn = \frac{Mn}{bd^2} = \frac{636.1 \times 10^6}{(0.9)(1000)(435.5)^2} = 3.73 \text{ Mpa}$$

$$A_s \text{ min} = \frac{\sqrt{28}}{4(420)} (1000)(435.5) = 1371.7 \text{ mm}^2$$

$$A_s \text{ min} = \frac{1.4}{420} (1000)(435.5) = 1451.67 \text{ mm}^2 \sim \text{control}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2mkn}{fy}} \right) = \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 3.73}{420}} \right) = 0.00971$$

65

$$A_s = 0.00971 (1000) (435.5) = 4228.71 \text{ mm}^2 > A_{s \text{ min}} = 1451.67 \text{ mm}^2$$

$$\# \text{ of bars} = A_s / A_{s \text{ bar}} = 4228.71 / 491 = 8.61 \quad * \text{ Note } A_{\Phi 25} = 491 \text{ mm}^2$$

Select bar 9 Φ 25

$$\text{Total } A_{s \text{ (provide)}} = 4419 \text{ mm}^2 > 4228.71 \text{ mm}^2$$

* Check strain for the magnitude of under strength factor Φ :

Tension = Compression

$$A_s \times fy = 0.85 \times f_c' \times b \times a$$

$$4419 \times 420 = 0.85 \times 28 \times 1000 \times a$$

$$a = 77.98 \text{ mm}$$

$$X = \frac{a}{0.85} = \frac{77.98}{0.85} = 91.7 \text{ mm}$$

$$\epsilon_s = \frac{435.5 - 91.7}{91.7} \times 0.003 = 0.0112$$

$$\epsilon_s = 0.0112 > 0.005$$

Ok.....

***Check for bar distance:**

$$S = \frac{1000 - 2 \times 40 - 2 \times 12 - 9 \times 25}{8} = 83.9 \text{ mm} > 25 \text{ mm} \dots \text{ok}$$

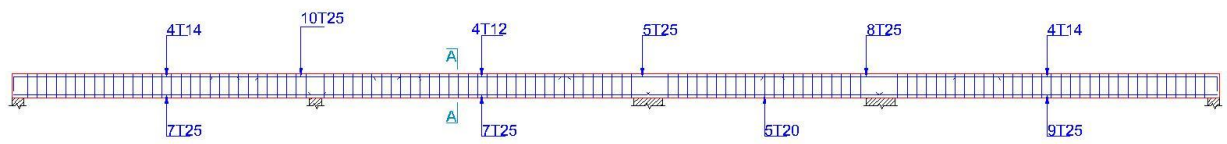


Figure (4.15) reinforcement for beam BG-26

4.3.8 Design of column G2

$$f'_c = 28 \text{ MPa}$$

$$F_y = 420 \text{ MPa}$$

The Column is an interior one.

$$\text{DL} = 1200 \text{ KN}$$

$$\text{LL} = 450 \text{ KN}$$

$$P_u = 1.2\text{DL} + 1.6\text{LL}$$

$$P_u = 1.2(1200) + 1.6(450)$$

$$\mathbf{P_u = 2160 \text{ KN}}$$

1- Check for slenderness:-

$$\frac{k l_n}{r} \leq 34 - 12 \left(\frac{M_1}{M_2} \right) \leq 40$$

$$*\frac{M_1}{M_2} = 1 \text{ braced frame with } M_{min}$$

K=1 for column in non-sway frames.

$$\frac{k l_n}{r} \leq 34 - 12 = 22 \leq 40$$

$$\frac{k l_n}{r_x} = \frac{1 \cdot 3.7}{0.3 \cdot 0.6} = 20.55 < 22 \text{ Column is short about x-axis}$$

$$\frac{k l_n}{r_y} = \frac{1 \cdot 3.7}{0.3 \cdot 0.4} = 30.83 > 22 \text{ Column is long about y-axis}$$

Nominal axial strength of column $P_n = P_{nx}$

2- Calculate the minimum eccentricity e_{min} and the minimum moment M_{min}

$$e_{x_{min}} = (15 + 0.03h) = 15 + 0.03 \cdot 600 = 33 \text{ mm}$$

$$P_{u_{factored}} = 2160 \text{ KN.}$$

$$M_{min} = P_u \cdot e_{x_{min}} = 2160 \cdot \frac{33}{1000} = 71.28 \text{ KN.}$$

3- Compute EI

$$I_g = \frac{bh^3}{12} = \frac{400 * 600^3}{12} = 0.72 * 10^{10} mm^4$$

$$\beta_{dns} = \frac{1.2 D (sustained)}{1.2D + 1.6L} = 0.666$$

$$EI = \frac{0.4 * 4750 \sqrt{f'c'} I_g}{1 + \beta_{dns}} = \frac{0.4 * 4750 \sqrt{28'} * 0.72 * 10^{10}}{1 + 0.666} = 43.45 MN/m^2$$

4- Determine the Euler buckling load, P_c :

$$P_c = \frac{\pi^2 EI}{(kl_n)^2} = \frac{\pi^2 * 43.45}{(1 * 3.7)^2} = 31.32 MN$$

5- Calculate the moment magnifier factor δ_{ns} :

$$C_m = 0.6 + 0.4 \frac{M_1}{M_2} = 0.6 + 0.4 * 1 = 1 > 0.4$$

$$\delta_{ns} = \frac{C_m}{1 - \frac{P_u}{0.75 P_c}} = \frac{1}{1 - \frac{2.160}{0.75 * 31.32}} = 1.101$$

$$1.4 > 1.101 > 1 \dots \dots \dots \text{ok}$$

The magnified eccentricity and moment:

$$e = e_{min} * \delta_{ns} = 33 * 1.101 = 36.333 mm$$

$$M_{ux} = \delta_{ns} * M_{ux} = 1.101 * 71.28 = 78.48 KN.m$$

6- Select column reinforcement

We will use the tide column interaction diagrams

$$\frac{ey}{h} = \frac{36.333}{600} = 0.0605$$

Compute ratio γ

$$\gamma = \frac{d - d'}{h} = \frac{600 - 2 * 40 - 2 * 10 - 18}{600} = 0.803$$

$$\frac{\phi P_n}{A_g} = \frac{P_u}{A_g} = \frac{2160 * 10^{-3}}{0.6 * 0.4} = 9 \text{ Mn/m}^2$$

$$\rho_g = 0.012$$

∴ select reinforcement

$$A_{st} = \rho_g A_g = 0.012 * 600 * 400 = 2880 \text{ mm}^2$$

$$A_s \phi 18 = 254.47 \text{ mm}^2$$

$$\frac{A_s}{A_s \phi 20} = 9.43$$

Use 12 ϕ 18 with $A_s = 3052 \text{ mm}^2 > 2800 \text{ mm}^2$ ok

*Design of ties

Use ties ϕ 10 with spacing of ties shall not exceed

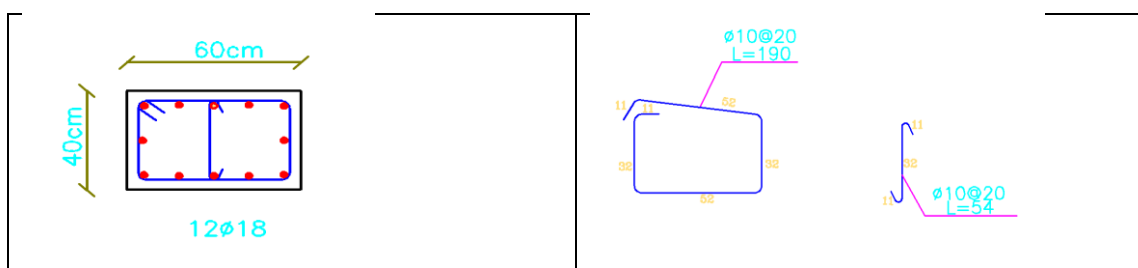
- 1) 48 times the tie diameter , $48d_s = 48 * 10 = 480 \text{ mm}$
- 2) 16 times the longitudinal bar diameter $16d_b = 16 * 18 = 288 \text{ mm}$ control
- 3) The least dimension of column = 400 mm

Use ties ϕ 10 @ 200 mm

1-Check for clear spacing between longitudinal bars

$$\text{Clear spacing} = \frac{600 - 40 * 2 - 10 * 2 - 2 * 16}{3} = 154.7 > 40 \text{ mm} > 1.5 * 18 = 27$$

80.8



(4.13) Design of footing:

$$P_u = 1146 \text{ KN} \dots f'_c = 28 \text{ Mpa}$$

Calculate the weight of footing, soil and the surcharge floor load

$$h_{\text{footing}} = 45 \text{ cm}$$

$$W_{\text{footing}} = 0.45 * 25 = 11.25 \text{ KN/m}^2$$

$$\text{Weight soil} = 0.45 * 18 = 8.1 \text{ KN/m}^2$$

Total surcharge load on foundation

$$W = 11.25 + 8.1 + 5 = 24.35 \text{ KN/m}^2$$

- **net soil pressure, $q_{a_{\text{net}}}$:**

$$q_{a_{\text{net}}} = 350 - 24.35 = 325.65 \text{ KN/m}^2$$

$$P_u = 1146 \text{ KN}$$

$$q_u = \frac{1146}{2 * 1.8} = 318.33 \text{ KN/m}^2$$

$$q_{bu} = 1.4 * q = 1.4 * 318.33 = 445.662 > q_{a_{\text{net}}} \dots \text{ok}$$

calculate d:

$$V_u = q_u * b \left(\frac{a}{2} - \frac{l}{2} - d \right) = 445.662 * 1.8 \left(\frac{2}{2} - \frac{0.55}{2} - d \right)$$

$$V_u = 581.59 - 802.19 d$$

$$V_c = \frac{1}{6} * \sqrt{f'_c} * b w * d = \frac{1}{6} * \sqrt{28} * 1800 * d = 1587.45 d$$

$$\phi V_c = V_u \dots \phi = 0.75$$

$$0.75 * 1587.45 = 1190.60$$

$$1190.60 d = 581.59 - 802.19 d$$

$$d = 0.260\text{m}$$

assume cover 50mm and steel bar $\phi 14$

$$h = 260 + 75 + 14 = 349\text{mm}$$

take $h = 450\text{mm}$

$$d = 450 - 75 - 14 = 361\text{mm}$$

- Punching shear

Let $V_u = \phi V_c$

$$V_u = 445.662(2 * 1.8 - 0.911 * 0.711)$$

$$V_u = 1315.72 \text{ KN}$$

$$B = \frac{550}{350} = 1.57$$

$$b_o = 2 * 91.1 + 2 * 71.1 = 3.244\text{m}$$

$$\alpha_s = 40 - \text{interior}$$

$$V_c = \frac{1}{6} * \left(1 + \frac{2}{B}\right) \sqrt{f'_c} * b_o * d \quad \text{where } \frac{1}{6} * \left(1 + \frac{2}{B}\right) = \frac{1}{6} * \left(1 + \frac{2}{1.57}\right) = .38$$

$$V_c = \frac{1}{12} \left(\frac{\alpha_s d}{b_o} + 2 \right) \sqrt{f'_c} * b_o * d \quad \text{where } \frac{1}{12} \left(\frac{\alpha_s d}{b_o} + 2 \right) = \frac{1}{12} \left(\frac{40 * 0.386}{3.244} + 2 \right) = 0.54$$

$$V_c = \frac{1}{3} * \sqrt{f'_c} * b_o * d \quad \text{where } \frac{1}{3} = 0.333 \dots \dots \dots \text{control}$$

$$\text{Take } V_c = \frac{1}{3} * \sqrt{f'_c} * b_o * d = \frac{1}{3} * \sqrt{28} * 3244 * 361 * 10^{-3} = 2065.6 \text{ KN}$$

$$\phi V_c = 0.75 * 2065.6 = 1549.2 \text{ KN}$$

$$\phi V_c = 1549.2 > V_u = 1315.72 \text{ KN} \dots \dots \dots \text{ok}$$

Design flexure in long direction

$$b = 2\text{m}$$

$$h = 450\text{mm}$$

$$d = 450 - 75 - 14/2 = 368$$

$$M_u = 445.662 * 2 * 0.541 * 0.541/2 = 130.44 \text{KN.m}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 * 28} = 17.65$$

$$R_n = \frac{M_u}{\phi b * d^2} = \frac{130.44 * 10^6}{0.9 * 2000 * (368)^2} = 0.535 \text{MPa.}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 * R_n * m}{f_y}} \right)$$

$$= \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.535}{420}} \right) = 0.0013$$

$$A_s = \rho * b * d = 0.0013 * 2000 * 368 = 956.8 \text{ mm}^2.$$

$$A_{smin} = 0.0018 * b * h = 0.0018 * 2000 * 450 = 1620 \text{mm}^2$$

$$A_{smin} = 1620 \text{ mm}^2 > A_{sreq} = 956.8 \text{mm}^2.$$

$$\therefore A_s = 1620 \text{ mm}^2.$$

$$n = \frac{A_{sreq}}{A_{bar} \phi 14} = \frac{1620}{154} + 1 = 11.52$$

$$\therefore \text{Use } 12\Phi 14 \text{ with } A_{spro} = 1848 \text{ mm}^2.$$

$$S = \frac{2000 - 75 * 2 - 12 * 14}{11} = 153 \text{mm}$$

Step S is the smallest of

$$1- 3h = 3 * 450 = 1350 \text{mm}$$

$$2- 450 \dots \dots \dots \text{control}$$

$$S = 153 < S_{max} = 450 \dots \dots \dots \text{ok}$$

Check of strain

$$a = \frac{A_s A_f}{0.85 f'_c b} = \frac{1848 * 420}{0.85 * 28 * 2000} = 16.3$$

$$c = \frac{a}{0.85} = \frac{16.3}{0.85} = 19.2$$

$$\epsilon = 0.003 \left(\frac{d - c}{c} \right) = 0.003 \left(\frac{361 - 19.2}{19.2} \right) = .0534 > 0.005 \dots \dots \dots \text{ok}$$

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- Design flexure for short direction:

Take steel bare of $\phi 14$

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$$b = 1800 \text{ mm} \quad h = 450 \text{ mm}$$

$$d = 450 - 75 - 14 - \frac{14}{2} = 354 \text{ mm}$$

$$f'_c = 28 \text{ MPa} \quad f_y = 420 \text{ MPa}$$

$$M_u = 445.662 * 1.8 * 0.548 * 0.548 / 2 = 120.45 \text{ KN.m}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 * 28} = 17.65$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{120.45 * 10^6}{0.9 * 1800 * (354)^2} = 0.593 \text{ MPa}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 R_n m}{f_y}} \right)$$

$$= \frac{1}{17.65} \left(1 - \sqrt{1 - \frac{2 * 17.65 * 0.593}{420}} \right) = 0.00143$$

$$A_s = \rho * b * d = 0.00143 * 1800 * 354 = 911.65 \text{ mm}^2$$

$$A_{s_{min}} = 0.0018 * b * h = 0.0018 * 1800 * 450 = 1458 \text{ mm}^2$$

$$A_{s_{min}} = 1458 \text{ mm}^2 > A_{s_{req}} = 911.65 \text{ mm}^2$$

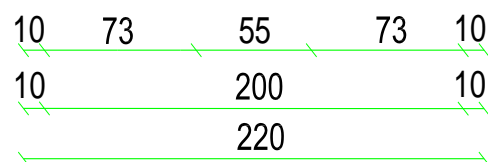
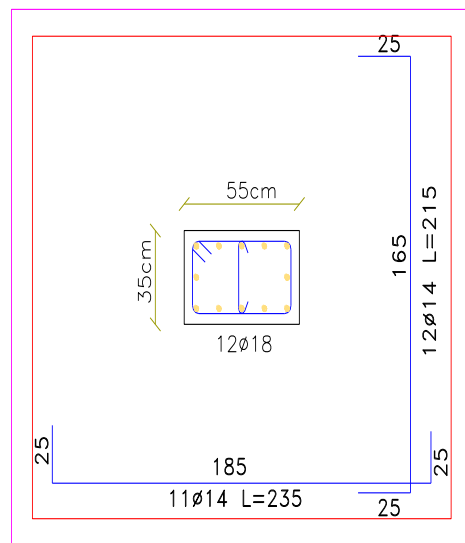
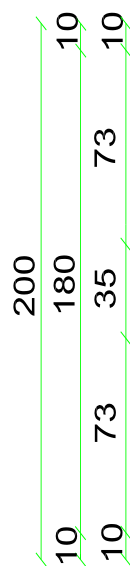
$$\therefore A_s = 1458 \text{ mm}^2$$

$$n = \frac{A_{s_{req}}}{A_{bar} \phi 14} = \frac{1458}{154} + 1 = 10.47$$

$$\therefore \text{Use } 11\Phi 14 \text{ with } A_s = 1694 \text{ mm}^2$$

$$S = \frac{1800 - 75 * 2 - 11 * 14}{10} = 149.6 \text{ mm}$$

$$S = 149.6 < S_{max} = 450 \dots \dots \dots ok$$



Design of stairs :

Design of flight :

Calculation of load :

-	density kn/m ²	Calculation kn/m
flight	25	$25 \cdot .25 / \cos 29.5 = 7.81$
plaster	22	$22 \cdot .02 / \cos 29.5 = 0.51$
horizontal mortar	22	$22 \cdot .03 \cdot 1 = 0.66$
horizontal tiles	23	$23 \cdot .07 \cdot 33 / 30 = 0.76$
vertical tiles	23	$23 \cdot .07 \cdot 17.5 / 30 = 0.4$
vertical mortar	22	$22 \cdot 0.03 \cdot 17.5 / 30 = 0.39$
triangle	25	$25 \cdot 0.17 / 2 = 2.1$
		$\Sigma = 12 \text{ kn/m}$

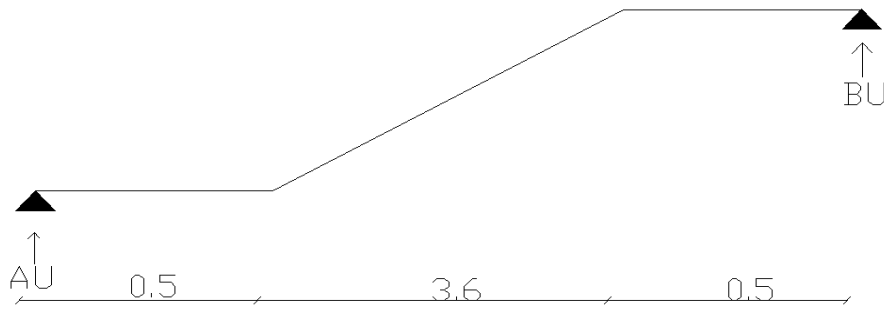
Calculation of h min:

h min: $4.1 / 20 = 20.5 \text{ cm}$
choose h = 25 cm

Design of flight :

dead load = 12 kn /m
live load = 5 kn /m

$q_u = 1.2 \cdot DD + 1.6 \cdot LL$
 $q_u = 1.2 \cdot 12 + 1.6 \cdot 5$
 $q_u = 22.4 \text{ kn /m}$



$$AU = BU = 22.4 \times 3.6 / 2 = 49.3 \text{ kN}$$

$$\text{Max } V_u = 40.3 \times \cos 29.5 = 35 \text{ kN}$$

$$\text{Max } m_u = 40.3 \times 2.3 - 22.4 \times 1.8 \times 0.9 = 56.4 \text{ kN.m}$$

Design for shear :

$$\text{Max } v_u = 35 \text{ kN}$$

$$d = 250 - 20 - 12/2 = 224 \text{ mm}$$

$$\phi V_c = 0.75 \times \frac{1}{6} \times 28^{.5} \times 1000 \times 224 = 148 \text{ kN}$$

$$\phi V_c \geq v_u$$

No shear reinforcement required

Design moment :

$$\text{Max } M_u = 56.4 \text{ kN.m}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 \times 28} = 17.65$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{56.4 \times 10^6}{0.9 \times 1000 \times (224)^2} = 1.25 \text{ MPa.}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 R_n m}{f_y}} \right) = 0.00305$$

$$A_s = \rho \times b \times d = 0.00305 \times 100 \times 224 = 6.85 \text{ cm}^2.$$

$$A_{s_{min}} = 0.0018 \times b \times h = 0.0018 \times 100 \times 25 = 4.5 \text{ cm}^2$$

$$\therefore A_s = 6.85 \text{ cm}^2.$$

Select 1Ø14 / 20cm

$$A_s = \pi/4 \cdot 1.4^2 \cdot 100/2 = 7.6 \geq A_{s \text{ req}}$$

Check strain :

$$A_s \cdot f_y = 0.85 \cdot f_c \cdot a \cdot b$$

$$\beta_1 = 0.85$$

$$7.69 \cdot 420 = 0.85 \cdot 28 \cdot a \cdot 100$$

$$a = 13.5 \text{ mm}$$

$$x = 13.5/0.85 = 15.96 \text{ mm}$$

strain

$$\left(\frac{d-x}{x}\right) \cdot 0.003 = 0.039 > 0.005 \text{ ok.}$$

$$\phi = 0.9$$

Design of landing :

Calculation of dead load :

material	density kn/m2	calculation
concrete	25	25*0.25 = 6.25
sand	16	16*0.07 = 1.1
mortar	22	22*0.02 = 0.4
tiles	23	23*0.03 = 0.7
plaster	22	22*.02 = 0.4
		$\Sigma = 8.85 \text{ kn/m}$

Dead load = 8.85 kn/m

Live load = 5 kn / m

Factoral load :

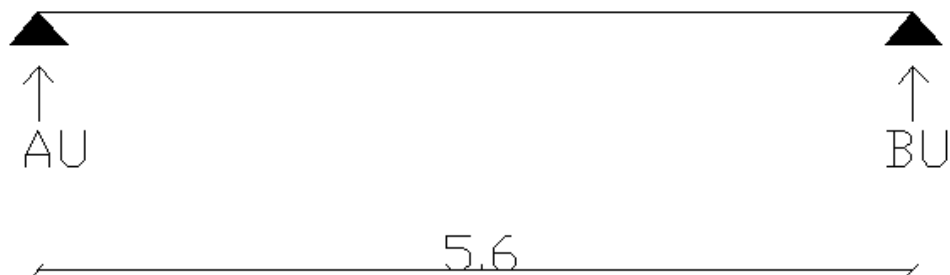
$$q_u = 1.2 \cdot DD + 1.6 \cdot LL$$

$$q_u = 1.2 \cdot 8.85 + 1.6 \cdot 5$$

$$q_u = 18.62 \text{ /m}$$

$$A_u = B_u \text{ from flight} = 40.3$$

$$40.3 + 18.62 = 58.92 \text{ kn/m}$$



$$A_u = B_u = 165 \text{ KN}$$

Analysis

$$\text{MAX } V_u = 165 - 58.92 \cdot 3.349 = 144.4 \text{ kn}$$

$$\text{MAX } M_u = (165 \cdot 5.6 / 2) - (58.92 \cdot 3.3 \cdot 1.65) = 223.6 \text{ KN} \cdot \text{M}$$

Design of shear:

$$\text{MAX } V_u = 144.4 \text{ kn}$$

$$\phi V_c = 0.75 \cdot \frac{1}{6} \cdot 28^{.5} \cdot 1000 \cdot 224 = 148 \text{ KN}$$

No shear reinforcement required .

Design of moment :

$$\text{MAX MU} = 223.6 \text{ KN. M}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 \cdot 28} = 17.65$$

$$R_n = \frac{M_u}{\phi b \cdot d^2} = \frac{223.6 \cdot 10^6}{0.9 \cdot 1000 \cdot (224)^2} = 4.95 \text{ MPa.}$$

$$\rho = \frac{1}{m} \left(1 - \sqrt{1 - \frac{2 \cdot R_n \cdot m}{f_y}} \right) = 0.01336$$

$$A_s = 30 \text{ cm}^2$$

$$A_s > A_{s \text{ min}}$$

$$\text{Use } 1\phi 18 / 10 \text{ cm}$$

Check strain :

$$A_s \cdot f_y = 0.85 \cdot f'_c \cdot a \cdot b$$

$$\beta_1 = 0.85$$

$$300 \cdot 420 = 0.85 \cdot 28 \cdot a \cdot 100$$

$$a = 52.9 \text{ mm}$$

$$x = 13.5 / 0.85 = 62.2 \text{ mm}$$

strain :

$$\left(\frac{d-x}{x} \right) 0.003 = 0.0077 > 0.005 \text{ ok.}$$

$$\phi = 0.9$$