

# **Chapter 4**

## **Structural Analysis & Design**

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## ✓ Introduction:

Concrete is the only major building material that can be delivered to the job site in a plastic state. This unique quality makes concrete desirable as a building material because it can be molded to virtually any form or shape.

Concrete used in most construction work is reinforced with steel. When concrete structure members must resist extreme tensile stresses, steel supplies the necessary strength. Steel is embedded in the concrete in the form of a mesh, or roughened or twisted bars. A bond forms between the steel and the concrete, and stresses can be transferred between both components.

In this project, all of design calculation for all structural members would be made upon the structural system which was chosen in the previous chapter.

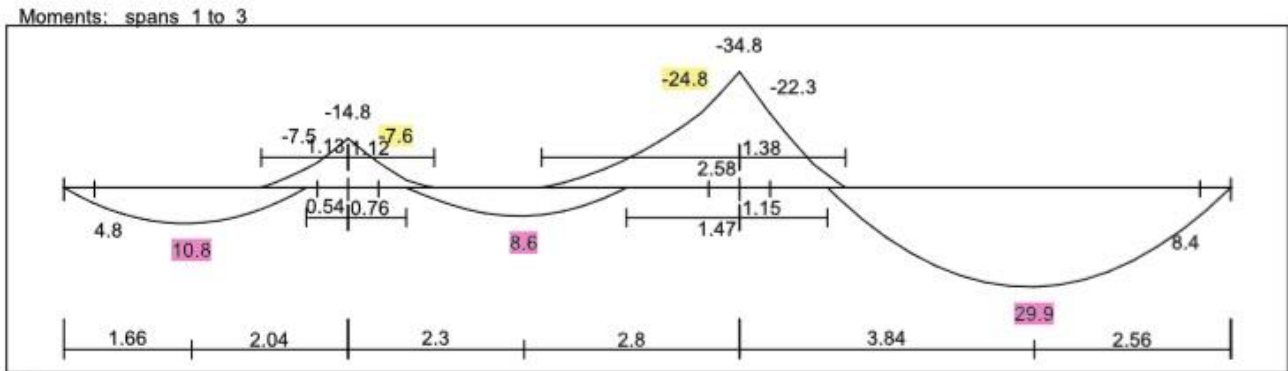
So, in this project, there are five types of slabs: One way solid slab, one way ribbed slab, two ribbed slab, flat slab, and waffle slab. They would be analyzed and designed by using finite element method of design, with aid of a computer program called "ATIR- Software " to find the internal forces, deflections and moments for ribbed slabs and by using the previous program and Etabs, Safe, And programs to find the internal forces.

## ✓ Factored loads:

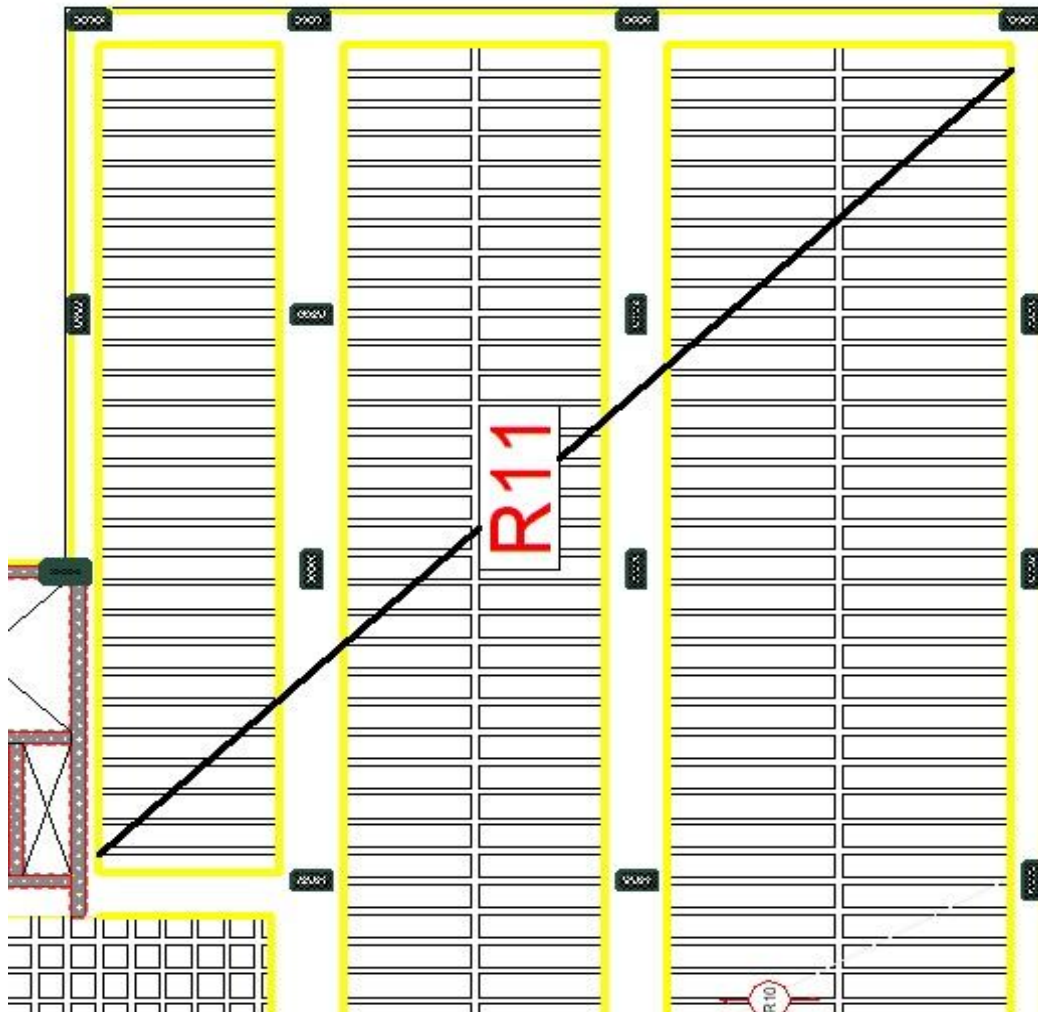
The factored loads on which the structural analysis and design is based for our project members, is determined as follows:

$$q_u = 1.2D.L + 1.6LL .$$

#### 4-1 Design of Rib 11:



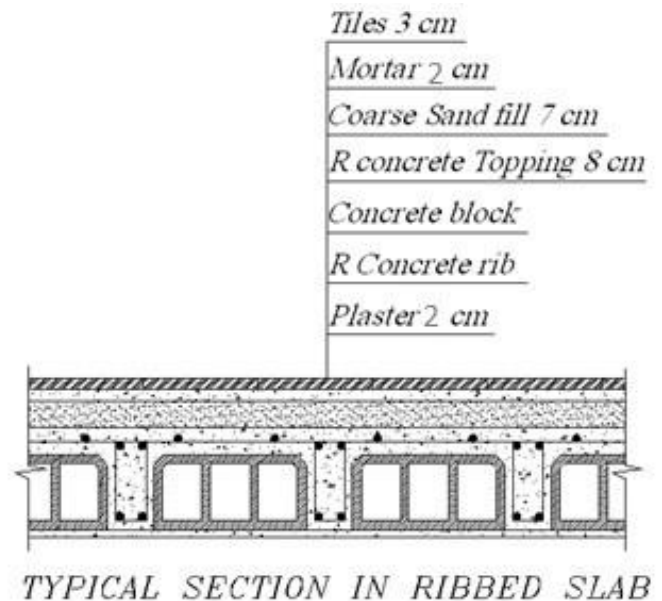
Fig(4-1):Moment Envelope (factored) units:KN.m



Fig(4.2): Rib 11

**Table ( 4.1) : Dead load calculation Topping**

Material	Quality Density KN/m <sup>3</sup>
Tiles	23
mortar	22
Sand	17
Reinforced Concrete	25
Hollow Block	10
Plaster	22
Partitions	1.5KN/m <sup>2</sup>



Compressive strength of concrete  $f_c' = 30 \text{ Mpa}$

Yield strength of steel ,  $f_y = 420 \text{ Mpa}$

Live Load, LL=3 KN/m<sup>2</sup>

✓ **Minimum thickness (deflection requirements):**

There are two groups of ribs and beams

The thickness of the one-way ribbed slab with drop beams can be obtained according to ACI code, table 9.5 (a).

The maximum span length for one-end continuous (for ribs):  $l = 640 \text{ cm}$  then

$$h_{min} = \frac{l}{18.5} = \frac{640}{18.5} = 34.6 \text{ cm}$$

The maximum span length for both-ends continuous (for ribs):  $l = 510 \text{ cm}$  then

$$h_{min} = \frac{l}{21} = \frac{510}{21} = 24.3 \text{ cm}$$

The minimum ribbed slab thickness will be  $h_{min} = 34.6 \text{ cm}$

Take slab thickness  $h = 35 \text{ cm} > h_{min} = 34.6 \text{ cm}$

$$h = 35 \text{ cm} \quad (27 \text{ cm HOLLOW BLOCK} + 8 \text{ cm TOPPING})$$

## ✓ 4-2 Topping Design:

Topping in One way ribbed slab can Be considered as a strip of **1 meter width** and span of hollow block length with both end fixed in the ribs.

**Dead Load calculations:**

Dead Load from:	$\delta \times \gamma \times 1$	KN/m
Tiles	$0.03 \times 23$	0.69
Mortar	$0.02 \times 22$	0.44
Coarse Sand	$0.07 \times 17$	1.19
Topping	$0.08 \times 25$	2
Interior Partitions	1.5	1.5
$\Sigma$		5.82

**Live Load calculations:**  $3 \times 1 = 3 \text{ KN/m}$

**Total Factored Load:**  $w_u = 1.2 \times 5.82 + 1.6 \times 3 = 11.78 \text{ KN/m}$

$$M_u = \frac{w u l^2}{12} = \frac{11.78 \times 0.4^2}{12} = 0.157 \text{ KN.m/m of strip width}$$

$\phi M_n \geq M_u$  Strength condition, where  $\phi = 0.55$  for plain concrete

$$M_n = 0.42 \lambda \sqrt{f_c'} S_m$$

where  $S_m$  for rectangular section of the slab:

$$S_m = \frac{b h^2}{6} = \frac{1000 \times 80^2}{6} = 1066666.67 \text{ mm}^3$$

$$M_n = 0.42 \lambda \sqrt{f_c'} S_m = 0.42 \times 1 \times \sqrt{30} \times 1066666.67 \times 10^{-6} = 2.45 \text{ KN.m}$$

$$\phi M_n = 0.55 \times 2.45 = 1.35 \text{ KN.m} \gg M_u = 0.157 \text{ KN.m}$$

NO Reinforcement is required by analysis. According to ACI 10.5.4., provide  $A_{s_{\min}}$  for slabs as shrinkage and temperature reinforcement.

$$\rho = 0.0018$$

$$AS = \rho b t = 0.0018 * 1000 * 80 = 144 \text{ mm}^2/\text{m strip}$$

Try bars  $\varnothing 8$  with  $AS = 50.27 \text{ mm}^2$

$$\text{Bar number } n = \frac{AS}{AS_{\varnothing 8}} = \frac{144}{50.27} = 2.87$$

Take 3  $\varnothing 8/\text{m}$  with  $AS = 150.8 \text{ mm}^2/\text{m strip}$  or  $\varnothing 8 @ 300 \text{ mm}$  in both direction  
step(s) is smallest of:

1.  $3h = 3 \times 80 = 240 \text{ mm}$  – control
2.  $450 \text{ mm}$
3.  $S =$

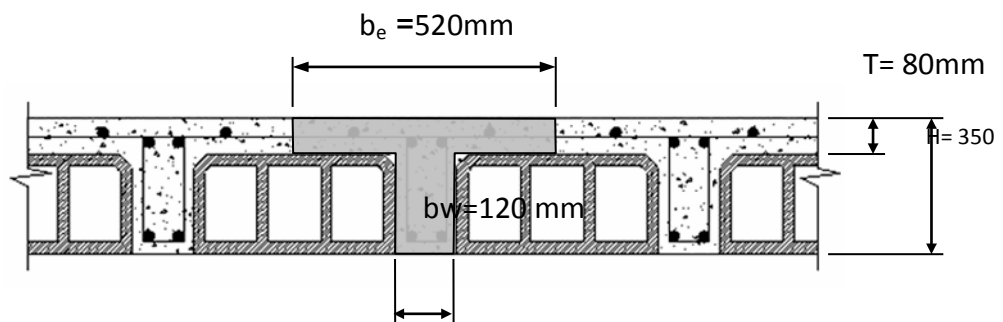
$$380 \left( \frac{280}{f_s} \right) - 2.5 C_c = 380 \left( \frac{280}{\frac{2}{3} 420} \right) - 2.5 * 20 =$$

**330 mm                      but**

$$S \leq 300 \left( \frac{280}{f_s} \right) = 300 \left( \frac{280}{\frac{2}{3} 420} \right) = 300 \text{ mm}$$

Take  $\varnothing 8 @ 200 \text{ mm}$  in both directions  $S = 200 \text{ mm} < S_{\max} = 240 \text{ mm}$  – ok

From practical consideration, the secondary reinforcement parallel to the ribs shall be placed in the slab and spaced at distances not more than half of the spacings between ribs (usually two bars upon each  $40 \text{ cm}$  width block).



✓ Load Calculations for Rib 11:

$$T = h_f = 80 \text{ mm}$$

$$b_w = 120 \text{ mm}$$

$$b_e = 520 \text{ mm}$$

$$h = 350 \text{ mm}$$

**Dead Load calculations**

Dead Load from:	$\delta \times \gamma \times b$	<i>KN.m</i>
Tiles	$0.03 \times 23 \times 0.52 =$	0.359
Mortar	$0.02 \times 22 \times 0.52 =$	0.2288
Coarse Sand	$0.07 \times 17 \times 0.52 =$	0.619
Topping	$0.08 \times 25 \times 0.52 =$	1.04
RC Rib	$0.27 \times 25 \times 0.12 =$	0.81
Hollow Block	$0.27 \times 10 \times 0.4 =$	1.08
Plaster	$0.02 \times 22 \times 0.52 =$	0.2288
Interior Partitions	$1.5 \times 0.52 =$	0.78
$\Sigma$		5.146

**Table(4-2):Dead Load Calculation of Rib (R 11)**

**Live Load calculations:**

$$LL = 3 \times 0.52 = 1.56 \text{ KN/m}$$

$$\text{Dead Load / rib: } DL = 5.146 \text{ KN.m}$$

$$\text{Live Load /rib: } LL = 1.56 \text{ KN.m}$$

✓ Design of Rib 11 for positive moments:

**1.Mu =+29.9KN.m**

\*Assume bar diameter  $\varnothing 14$  for main positive reinforcement.

$$d = h - \text{cover} - d_{\text{strip}} - \frac{db}{2} = 350 - 20 - 10 - \frac{14}{2} = 313 \text{ mm}$$

\*Check if  $a > h_f$

$$M_{nf} = 0.85 f_c' b h_f \left( d - \frac{h_f}{2} \right)$$

$$= 0.85 \times 30 \times 520 \times 80 \left( 313 - \frac{80}{2} \right) \times 10^{-6} = 289.6 \text{ KN.m}$$

$$M_{nf} = 289.6 \text{ KN.m} \gg \frac{Mu}{\phi} = \frac{29.9}{0.9} = 33.2 \quad a < h_f$$



**\*Design:**

$$R_n = \frac{Mu}{bd^2\phi} = \frac{29.9 \cdot 10^6}{0.9 \cdot 520 \cdot 313^2} = 0.652 \text{ MPa}$$

$$M = \frac{fy}{0.85 fc'} = \frac{420}{0.85 \cdot 30} = 16.47$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2R_n m}{fy}} \right) = \frac{1}{16.47} \left( 1 - \sqrt{1 - \frac{2 \cdot 0.652 \cdot 16.47}{420}} \right) = 0.00157$$

$$As = \rho b d = 0.00157 \cdot 520 \cdot 313 = 255.5 \text{ mm}^2$$

**\*Check for  $As_{min}$  :**

$$As_{min} = 0.25 \frac{\sqrt{fc'}}{fy} bw d \geq \frac{1.4}{fy} bw d$$

$$As_{min} = 0.25 \frac{\sqrt{30'}}{420} \cdot 120 \cdot 313 = 122.46 \text{ mm}^2$$

$$As_{min} = \frac{1.4}{420} \cdot 120 \cdot 313 = 125.2 \text{ mm}^2 \text{ -----Control}$$

$$As = 255.5 \text{ mm}^2 > As_{min} = 125.2 \text{ mm}^2 \text{ ---- OK}$$

$$\text{use } 2 \text{ } \phi 14 \text{ with } As = 3.08 \text{ cm}^2 > As_{req} = 2.56 \text{ cm}^2 \text{ ---- OK}$$

**\*Check for strain (Tension-Controlled section-  $\epsilon_s \geq 0.005$ ):**

$$a = \frac{As fy}{0.85 fc' b} = \frac{3.08 \cdot 420}{0.85 \cdot 30 \cdot 520} = 9.76 \text{ mm}$$

$$C = \frac{a}{\beta} \quad \beta = 0.836$$

$$C = \frac{9.76}{0.836} = 11.67 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d-c}{c} \right) = 0.003 \left( \frac{313-11.67}{11.67} \right) = 0.0775 > 0.005 \text{ ---- OK}$$

## **2. Mu = +10.8 KN.m**

**\*Assume bar diameter  $\phi 12$  for main positive reinforcement:**

$$d = h - \text{cover} - d_{strip} - \frac{db}{2} = 350 - 20 - 10 - \frac{12}{2} = 314 \text{ mm}$$

**\*Check if  $a > h_f$**

$$M_{nf} = 0.85 fc' b hf \left( d - \frac{hf}{2} \right)$$

$$= 0.85 \cdot 30 \cdot 520 \cdot 80 \left( 314 - \frac{80}{2} \right) \cdot 10^{-6} = 290.7 \text{ KN.m}$$

$$M_{nf}=290.7\text{KN.m} \gg \frac{Mu}{\phi} = \frac{10.8}{0.9} = 12 \quad a < hf$$

**\*Design:**

$$R_n = \frac{Mu}{bd^2\phi} = \frac{10.8 \cdot 10^6}{0.9 \cdot 520 \cdot 314^2} = 0.234 \text{ MPa}$$

$$M = \frac{fy}{0.85 f_c'} = \frac{420}{0.85 \cdot 30} = 16.47$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2R_n m}{fy}} \right) = \frac{1}{16.47} \left( 1 - \sqrt{1 - \frac{2 \cdot 0.234 \cdot 16.47}{420}} \right) = 0.00056$$

$$As = \rho b d = 0.00056 \cdot 520 \cdot 314 = 91.4 \text{ mm}^2$$

**\*Check for  $As_{min}$**

$$As_{min} = 0.25 \frac{\sqrt{f_c'}}{fy} bw d \geq \frac{1.4}{fy} bw d$$

$$As_{min} = 0.25 \frac{\sqrt{30}}{420} \cdot 120 \cdot 314 = 122.8 \text{ mm}^2$$

$$As_{min} = \frac{1.4}{420} \cdot 120 \cdot 314 = 125.6 \text{ mm}^2 \quad \text{-----Control}$$

$$As = 91.4 \text{ mm}^2 < As_{min} = 125.6 \text{ mm}^2$$

**use 2  $\phi 10$  with  $As = 1.57 \text{ cm}^2 > AS_{min} = 1.26 \text{ cm}^2$  ---- OK**

**\*Check for strain (Tension-Controlled section-  $\epsilon_s \geq 0.005$ ):**

$$a = \frac{As fy}{0.85 f_c b'} = \frac{1.57 \cdot 420}{0.85 \cdot 30 \cdot 520} = 4.97 \text{ mm}$$

$$C = \frac{a}{\beta} \quad \beta = 0.836$$

$$C = \frac{4.97}{0.836} = 5.95 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d-c}{c} \right) = 0.003 \left( \frac{315-5.95}{5.95} \right) = 0.156 > 0.005 \quad \text{---- OK}$$

Usually, no Reinforcement less than **2 $\phi 10$**  can be used .So for other span with positive moment equal 8.6 KN.m, use **2 $\phi 10$**  for rib span .

✓ **Design of Rib 11 for negative moments:**

**1.Mu = -24.8KN.m**

**\*Assume bar diameter  $\phi 14$  for main negative reinforcement:**

$$d = h - \text{cover} - d_{\text{strip}} - \frac{db}{2} = 350 - 20 - 10 - \frac{14}{2} = 313 \text{ mm}$$

**\*Design:**

$$R_n = \frac{Mu}{bd^2\phi} = \frac{24.8 \cdot 10^6}{0.9 \cdot 120 \cdot 313^2} = 2.34 \text{ MPa}$$

$$M = \frac{fy}{0.85 f_c'} = \frac{420}{0.85 \cdot 30} = 16.47$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2R_n m}{fy}} \right) = \frac{1}{16.47} \left( 1 - \sqrt{1 - \frac{2 \cdot 2.34 \cdot 16.47}{420}} \right) = 0.00585$$

$$A_s = \rho b d = 0.00585 \cdot 120 \cdot 313 = 219.86 \text{ mm}^2$$

**\*Check for  $A_{s\min}$**

$$A_s = 219.86 \text{ mm}^2 > A_{s\min} = 125.2 \text{ mm}^2 \quad \text{---- OK}$$

$$\text{use } 2 \text{ } \phi 14 \text{ with } A_s = 3.08 \text{ cm}^2 > A_{s\text{ req}} = 2.19 \text{ cm}^2 \text{ --- ok}$$

**\*Check for strain (Tension-Controlled section-  $\epsilon_s \geq 0.005$ ):**

$$a = \frac{A_s fy}{0.85 f_c' b} = \frac{3.08 \cdot 420}{0.85 \cdot 30 \cdot 120} = 42.26 \text{ mm}$$

$$C = \frac{a}{\beta} \quad \beta = 0.836$$

$$C = \frac{42.26}{0.836} = 50.55 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d-c}{c} \right) = 0.003 \left( \frac{313-50.55}{50.55} \right) = 0.0156 > 0.005 \quad \text{---- OK}$$

## **2. $M_u = -7.6 \text{ kN.m}$**

**\*Assume bar diameter  $\phi 12$  for main negative reinforcement:**

$$d = h - \text{cover} - d_{\text{strip}} - \frac{db}{2} = 350 - 20 - 10 - \frac{12}{2} = 314 \text{ mm}$$

**\*Design:**

$$R_n = \frac{Mu}{bd^2\phi} = \frac{7.6 \cdot 10^6}{0.9 \cdot 120 \cdot 314^2} = 0.714 \text{ MPa}$$

$$M = \frac{fy}{0.85 f_c'} = \frac{420}{0.85 \cdot 30} = 16.47$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2R_n m}{fy}} \right) = \frac{1}{16.47} \left( 1 - \sqrt{1 - \frac{2 \cdot 0.714 \cdot 16.47}{420}} \right) = 0.00172$$

$$A_s = \rho b d = 0.00172 \cdot 120 \cdot 314 = 64.81 \text{ mm}^2$$

\*Check for  $A_{s_{min}}$

$$A_{s_{min}} = 0.25 \frac{\sqrt{f_c'}}{f_y} b w d \geq \frac{1.4}{f_y} b w d$$

$$A_{s_{min}} = 0.25 \frac{\sqrt{30'}}{420} * 120 * 314 = 122.8 \text{ mm}^2$$

$$A_{s_{min}} = \frac{1.4}{420} * 120 * 314 = 125.6 \text{ mm}^2 \quad \text{-----Control}$$

$$A_s = 64.81 \text{ mm}^2 < A_{s_{min}} = 125.6 \text{ mm}^2$$

**use 2  $\phi 10$  with  $A_s = 1.57 \text{ cm}^2 > A_{s_{min}} = 1.26 \text{ cm}^2$  ---- OK**

\*Check for strain (Tension-Controlled section-  $\epsilon_s \geq 0.005$ ):

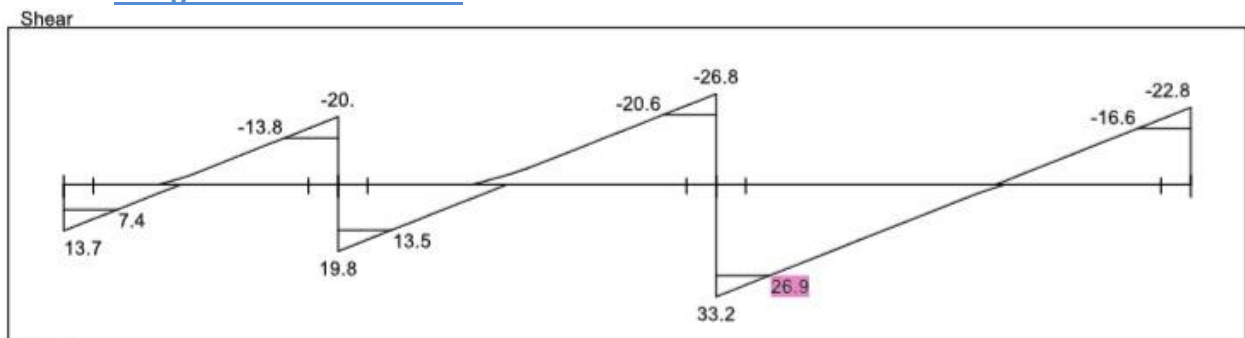
$$a = \frac{A_s f_y}{0.85 f_c b} = \frac{1.57 * 420}{0.85 * 30 * 120} = 21.55 \text{ mm}$$

$$C = \frac{a}{\beta} \quad \beta = 0.836$$

$$C = \frac{21.55}{0.836} = 25.78 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d-c}{c} \right) = 0.003 \left( \frac{315-25.78}{25.78} \right) = 0.0337 > 0.005 \quad \text{---- OK}$$

✓ Design of Rib 11 for shear:



**Fig(4-3) Shear Envelope (factored) units:KN**

The maximum shear force at the distance  $d$  from the face of support  $V_u = 26.9 \text{ KN}$ .

Shear strength,  $V_c$ , provided by concrete for the ribs may be taken 10% greater than that for beams. This is mainly due to the interaction between the slab and the closely spaced ribs.

$$V_n = \frac{V_u}{\phi}$$

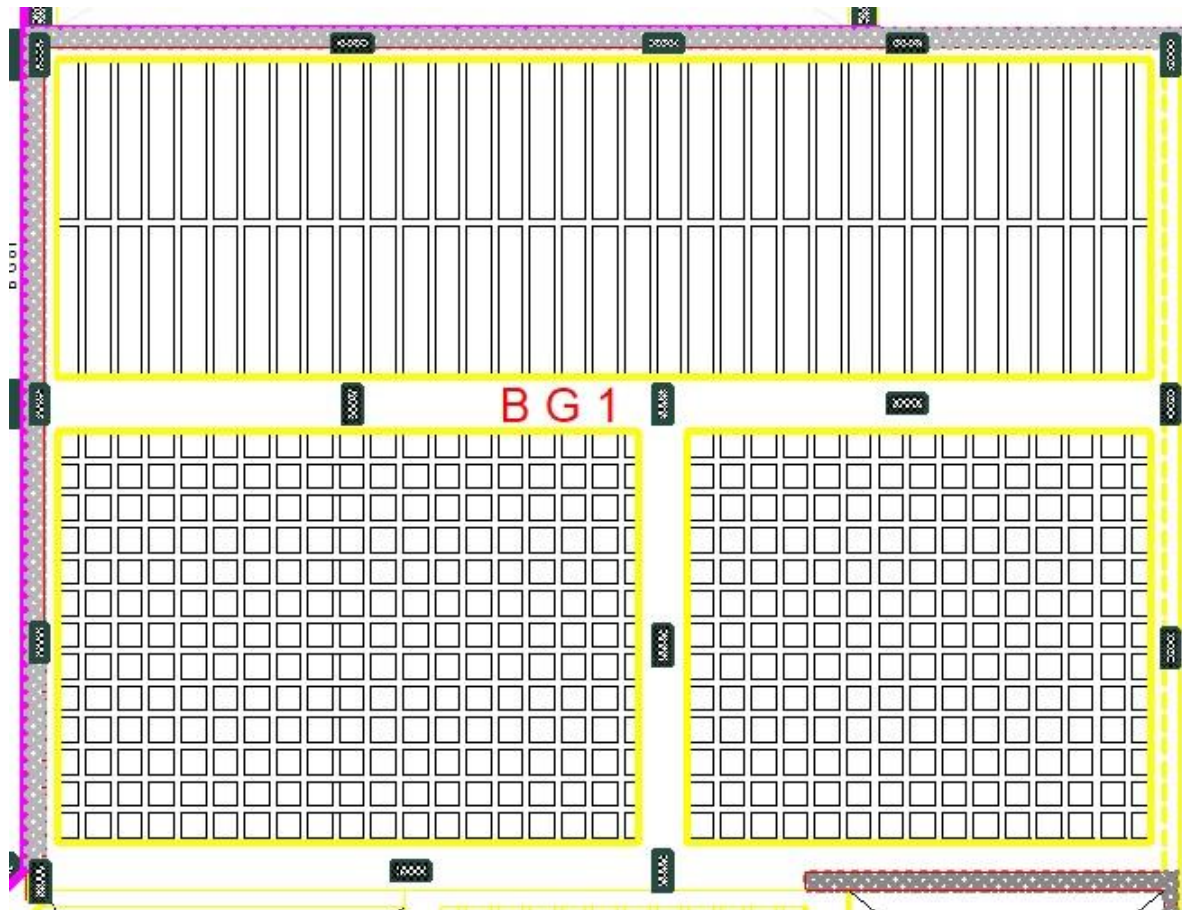
$$V_c = 1.1 * \frac{1}{6} \lambda \sqrt{f_c'} b_w d = 1.1 * \frac{1}{6} * 1 \sqrt{30} * 120 * 314 * 10^{-3} = 37.84 \text{ KN}$$

$$\phi V_c = 0.75 * 37.84 = 28.38 \text{ KN}$$

$$V_u = 26.9 \text{ KN} < \phi V_c = 28.38 \text{ KN}$$

→ Minimum Shear reinforcement is required **except for concrete joist construction**. So, no shear reinforcement is provided.

#### 4-3 Design of Beam B G 1 :



**Fig(4.4): Beam B G 1**

### Dead load from two way ribbed slab

Parts of Flight	Calculation
Tiles	$22 \times 0.03 \times 0.52 \times 0.52 = 0.178 \text{ KN}$
Mortar	$22 \times 0.02 \times 0.52 \times 0.52 = 0.119 \text{ KN}$
Sand	$16 \times 0.07 \times 0.52 \times 0.52 = 0.303 \text{ KN}$
Topping	$25 \times 0.08 \times 0.52 \times 0.52 = 0.541 \text{ KN}$
Rib	$25 \times 0.27 \times 0.12 \times (0.52 + 0.4) = 0.745 \text{ KN}$
Block	$9 \times 0.27 \times 0.4 \times 0.4 = 0.389 \text{ KN}$
Plaster	$22 \times 0.02 \times 0.52 \times 0.52 = 0.119 \text{ KN}$
	<div>Sum</div> <div>2.80 KN</div>

**Table ( 4.3) : Dead load from two way ribbed slab**

$$DL = 2.8 / (0.52 \times 0.52) = 10.36 \text{ KN/m}^3$$

$$LL = 3 \text{ KN/m}^3$$

$$\text{Dead Load from Two Way Ribbed Slab on Beam} = 2 \times 3.37 \times 10.36 = 69.83 \text{ KN/m}$$

$$\text{Live Load from Two Way Ribbed Slab on Beam} = 1 \times 3.37 \times 3 = 10.11 \text{ KN/m}$$

$$\text{Dead Load from One Ribbed Slab on Beam} = 5.146 \text{ KN/m}$$

$$\text{Live Load from One Ribbed Slab on Beam} = 1.56 \text{ KN/m}$$

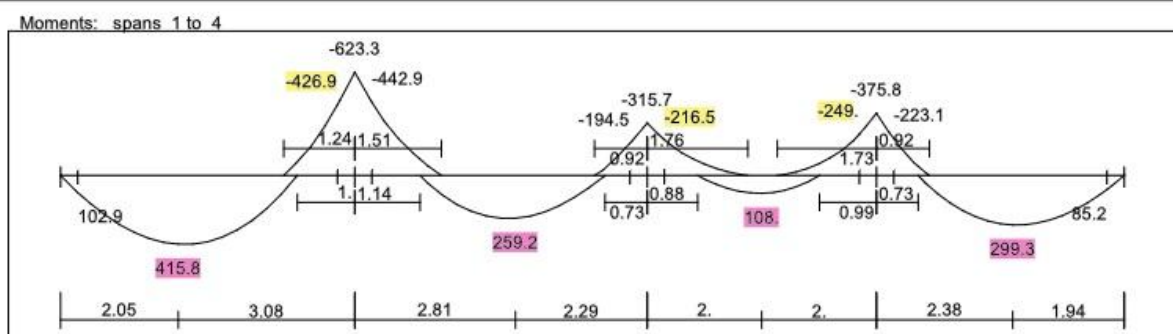
**Dead load of Beam:**

Material	W(KN/m)
Tiles	$22 \times 0.03 \times 0.8 = 0.528$
Mortar	$22 \times 0.02 \times 0.8 = 0.352$
Sand	$16 \times 0.07 \times 0.8 = 0.896$
Plaster	$22 \times 0.02 \times (0.8 + 0.3) = 0.484$
Partitions $1.5 \text{ KN/m}^2$	$1.5 \times 0.8 = 1.2$
Total Dead Load ,KN	3.46

**Table ( 4.4) : Dead load of Beam**

Service DD upon the Beam= $3.46+0.8\times0.5\times25=13.46$  KN/m

Service LL upon the Beam =  $3 \times 0.8 = 2.4 \text{ kN/m}$



**Fig(4-5) :Moment Envelope (factored) units:KN.m**



✓ Design of Positive Moment :

**MAX. Positive Moment=108 KN.m**

$$bw = 80cm, h = 50cm$$

$$d = 500 - 40 - 10 - 12.5 = 437.5mm$$

$$Mu = 108 \text{ KN.m}$$

$$Mn = \frac{Mu}{\Phi} = \frac{108}{0.9} = 120 \text{ KN.m}$$

$$As_{min} = \frac{\sqrt{fc'}}{4(fy)}(bw)(d) \geq \frac{1.4}{fy}(bw)(d).$$

$$As_{min} = \frac{\sqrt{30}}{4(420)}(800)(437.5) \geq \frac{1.4}{420}(800)(437.5)$$

$$As_{min} = 1141.1mm^2 < 1166.7mm^2 \dots\dots\dots\text{the larger is control}$$

$$As_{min} = 1166.7mm^2$$

$$Rn = \frac{Mn}{b * d^2}$$

$$Rn = \frac{120}{800 * 437.5^2} = 0.784 \text{ Mpa}$$

$$m = \frac{fy}{0.85 * fc'} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mRn}{fy}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(0.784)}{420}} \right) = 0.001896$$

$$A_{req} = \rho * b * d = 0.001896 * 800 * 437.5 = 663.72 \text{ mm}^2$$

$$663.72 \text{ mm}^2 < As_{min} = 1166.7mm^2$$

$$A_{min} = As$$

$$\text{Use } 3 \Phi 25 >> \# \text{ of bar} = \frac{1166.7}{491} = 3$$

Then we select 3 bars  $\Phi 25$   $A_{s,provided} = 3 * 491 = 1472.62 mm^2$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c * b * a$$

$$1472.62 * 420 = 0.85 * 30 * 800 * a$$

$$a = 30.32 mm$$

$$\beta_1 = 0.85 - 0.007(f_c - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{30.32}{0.836} = 36.27 mm$$

$$\varepsilon_s = \frac{437.5 - 36.27}{36.27} \times 0.003$$

$$\varepsilon_s = 0.033 > 0.005$$

$$\Phi * M_n = \Phi * A_s * f_y * (d - \frac{a}{2})$$

$$\Phi * M_n = 0.9 * 1166.7 * 420 * (437.5 - 15.16) = 186.25 > 108 \text{ singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 3 * 25}{2}$$

$$S = 332.5 mm \geq 25 mm$$

### ✓ Design of Positive Moment :

**MAX. Positive Moment=415.8 KN.m**

$$bw = 80 cm, h = 50 cm$$

$$d = 500 - 40 - 10 - 12.5 = 437.5 mm$$

$$M_u = 415.8 \text{ KN.m}$$

$$M_n = \frac{M_u}{\Phi} = \frac{415.8}{0.9} = 462 \text{ KN.m}$$

$$A_{s_{\min}} = \frac{\sqrt{f_c'}}{4(f_y)}(bw)(d) \geq \frac{1.4}{f_y}(bw)(d).$$

$$A_{s_{\min}} = \frac{\sqrt{30}}{4(420)}(800)(437.5) \geq \frac{1.4}{420}(800)(437.5)$$

$$A_{s_{\min}} = 1141.1 \text{ mm}^2 < 1166.7 \text{ mm}^2 \dots\dots\dots \text{the larger is control}$$

$$A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$R_n = \frac{M_n}{b * d^2}$$

$$R_n = \frac{462}{800 * 437.5^2} = 3.02 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 * f_c'} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(3.02)}{420}} \right) = 0.007677$$

$$A_{\text{req}} = \rho * b * d = 0.007677 * 800 * 437.5 = 2686.95 \text{ mm}^2$$

$$2686.95 \text{ mm}^2 > A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$\text{Use } 6 \Phi 25 \gg \# \text{ of bar} = \frac{2945.22}{491} = 6$$

$$\text{Then we select 6 bars } \Phi 25 \quad A_{s_{\text{provided}}} = 6 * 491 = 2945.22 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c' * b * a$$

$$2945.22 * 420 = 0.85 * 30 * 800 * a$$

$$a = 60.6mm$$

$$\beta_1 = 0.85 - 0.007(fc - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{60.6}{0.836} = 72.5mm$$

$$\varepsilon_s = \frac{437.5 - 72.5}{72.5} \times 0.003$$

$$\varepsilon_s = 0.015 > 0.005$$

$$\Phi * Mn = \Phi * As * fy * (d - \frac{a}{2})$$

$$\Phi * Mn = 0.9 * 2945.22 * 420 * (437.5 - 30.3) = 453.33 > 415.8 \dots \text{singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 6 * 25}{5}$$

$$S = 110mm \geq 25mm$$

### MAX. Positive Moment=259.2 KN.m

$$bw = 80cm, h = 50cm$$

$$d = 500 - 40 - 10 - 12.5 = 437.5mm$$

$$Mu = 259.2 \text{ KN.m}$$

$$Mn = \frac{Mu}{\Phi} = \frac{259.2}{0.9} = 288 \text{ KN.m}$$

$$As_{min} = \frac{\sqrt{fc'}}{4(fy)} (bw)(d) \geq \frac{1.4}{fy} (bw)(d)$$

$$As_{min} = \frac{\sqrt{30}}{4(420)} (800)(437.5) \geq \frac{1.4}{420} (800)(437.5)$$

$$As_{min} = 1141.1mm^2 < 1166.7mm^2 \dots \text{the larger is control}$$

$$A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$R_n = \frac{M_n}{b * d^2}$$

$$R_n = \frac{288}{800 * 437.5^2} = 1.88 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 * f_c} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(1.88)}{420}} \right) = 0.00465$$

$$A_{\text{req}} = \rho * b * d = 0.00465 * 800 * 437.5 = 1629.23 \text{ mm}^2$$

$$1629.23 \text{ mm}^2 > A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$\text{Use } 4 \Phi 25 \gg \# \text{ of bar} = \frac{1629.23}{491} = 4$$

$$\text{Then we select 4 bars } \Phi 25 \text{ } A_{s_{\text{provided}}} = 4 * 491 = 1963.5 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c * b * a$$

$$1963.5 * 420 = 0.85 * 30 * 800 * a$$

$$a = 40.42 \text{ mm}$$

$$\beta_1 = 0.85 - 0.007(f_c - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{40.42}{0.836} = 48.36 \text{ mm}$$

$$\epsilon_s = \frac{437.5 - 48.36}{48.36} \times 0.003$$

$$\epsilon_s = 0.024 > 0.005$$

$$\Phi * M_n = \Phi * A_s * f_y * \left( d - \frac{a}{2} \right)$$

$$\Phi * Mn = 0.9 * 1963.5 * 420 * (437.5 - 20.21) = 309.72 > 259.2 \quad \text{singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 4 * 25}{3}$$

$$S = 200 \text{ mm} \geq 25 \text{ mm}$$

### MAX. Positive Moment=299.3 KN.m

$$bw = 80 \text{ cm}, h = 50 \text{ cm}$$

$$d = 500 - 40 - 10 - 12.5 = 437.5 \text{ mm}$$

$$Mu = 299.3 \text{ KN.m}$$

$$Mn = \frac{Mu}{\Phi} = \frac{299.3}{0.9} = 332.56 \text{ KN.m}$$

$$As_{\min} = \frac{\sqrt{fc'}}{4(fy)} (bw)(d) \geq \frac{1.4}{fy} (bw)(d).$$

$$As_{\min} = \frac{\sqrt{30}}{4(420)} (800)(437.5) \geq \frac{1.4}{420} (800)(437.5)$$

$$As_{\min} = 1141.1 \text{ mm}^2 < 1166.7 \text{ mm}^2 \dots\dots\dots \text{the larger is control}$$

$$As_{\min} = 1166.7 \text{ mm}^2$$

$$Rn = \frac{Mn}{b * d^2}$$

$$Rn = \frac{332,56}{800 * 437.5^2} = 2.17 \text{ Mpa}$$

$$m = \frac{fy}{0.85 * fc'} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mRn}{fy}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(2.17)}{420}} \right) = 0.00541$$

$$A_{\text{req}} = \rho * b * d = 0.00541 * 800 * 437.5 = 1894.42 \text{ mm}^2$$

$$1894.42 \text{ mm}^2 > A_{s_{\text{min}}} = 1166.7 \text{ mm}^2$$

$$\text{Use } 4 \Phi 25 \gg \# \text{ of bar} = \frac{1894.41}{491} = 4$$

$$\text{Then we select 4 bars } \Phi 25 \quad A_{s_{\text{provided}}} = 4 * 491 = 1963.5 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c * b * a$$

$$1963.5 * 420 = 0.85 * 30 * 800 * a$$

$$a = 40.42 \text{ mm}$$

$$\beta_1 = 0.85 - 0.007(f_c - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{40.42}{0.836} = 48.36 \text{ mm}$$

$$\varepsilon_s = \frac{437.5 - 48.36}{48.36} \times 0.003$$

$$\varepsilon_s = 0.024 > 0.005$$

$$\Phi * Mn = \Phi * A_s * f_y * \left(d - \frac{a}{2}\right)$$

$$\Phi * Mn = 0.9 * 1963.5 * 420 * (437.5 - 20.21) = 309.72 > 259.2 \quad \text{singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 4 * 25}{3}$$

$$S = 200 \text{ mm} \geq 25 \text{ mm}$$

✓ Design of Negative Moment :

**MAX. Negative Moment=442.9 KN.m**

$$bw = 80cm, h = 50cm$$

$$d = 437.5mm$$

$$Mu = 442.9KN .m$$

$$Mn = \frac{Mu}{\Phi} = \frac{442.9}{0.9} = 492.11 \text{ KN .m}$$

$$As_{min} = \frac{\sqrt{fc'}}{4(fy)}(bw)(d) \geq \frac{1.4}{fy}(bw)(d).$$

$$As_{min} = \frac{\sqrt{30}}{4(420)}(800)(437.5) \geq \frac{1.4}{420}(800)(437.5)$$

$$As_{min} = 1141.1mm^2 < 1166.7mm^2 \dots\dots\dots\text{the larger is control}$$

$$As_{min} = 1166.7mm^2$$

$$Rn = \frac{Mn}{b * d^2}$$

$$Rn = \frac{492.11}{800 * 437.5^2} = 3.21Mpa$$

$$m = \frac{fy}{0.85 * fc'} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mRn}{fy}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(3.21)}{420}} \right) = 0.008197$$

$$A_{req} = \rho * b * d = 0.008197 * 800 * 437.5 = 2868.95 \text{ mm}^2$$

$$2868.95 \text{ mm}^2 > As_{min} = 1166.7mm^2$$



$$\text{Use } 6 \Phi 25 \gg \# \text{ of bar} = \frac{2945.22}{491} = 6$$

$$\text{Then we select 6 bars } \Phi 2, A_{s \text{ provided}} = 6 * 491 = 2945.22 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c * b * a$$

$$2945.22 * 420 = 0.85 * 30 * 800 * a$$

$$a = 60.6 \text{ mm}$$

$$\beta_1 = 0.85 - 0.007(f_c - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{60.6}{0.836} = 72.5 \text{ mm}$$

$$\varepsilon_s = \frac{437.5 - 72.5}{72.5} \times 0.003$$

$$\varepsilon_s = 0.015 > 0.005$$

$$\Phi * M_n = \Phi * A_s * f_y * (d - \frac{a}{2})$$

$$\Phi * M_n = 0.9 * 2945.22 * 420 * (437.5 - 30.3) = 453.33 > 442.9 \text{ singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 6 * 25}{5}$$

$$S = 110 \text{ mm} \geq 25 \text{ mm}$$

### MAX. Negative Moment=249 KN.m

$$b_w = 80 \text{ cm}, h = 50 \text{ cm}$$

$$d = 437.5 \text{ mm}$$

$$M_u = 249 \text{ KN.m}$$

$$M_n = \frac{M_u}{\Phi} = \frac{249}{0.9} = 276.67 \text{ KN.m}$$

$$A_{s_{\min}} = \frac{\sqrt{f_c'}}{4(f_y)}(bw)(d) \geq \frac{1.4}{f_y}(bw)(d).$$

$$A_{s_{\min}} = \frac{\sqrt{30}}{4(420)}(800)(437.5) \geq \frac{1.4}{420}(800)(437.5)$$

$$A_{s_{\min}} = 1141.1 \text{ mm}^2 < 1166.7 \text{ mm}^2 \dots\dots\dots \text{the larger is control}$$

$$A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$R_n = \frac{M_n}{b * d^2}$$

$$R_n = \frac{276.67}{800 * 437.5^2} = 1.81 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 * f_c'} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(1.81)}{420}} \right) = 0.00447$$

$$A_{\text{req}} = \rho * b * d = 0.00447 * 800 * 437.5 = 1563.27 \text{ mm}^2$$

$$1563.27 \text{ mm}^2 > A_{s_{\min}} = 1166.7 \text{ mm}^2$$

$$\text{Use } 4 \Phi 25 \gg \# \text{ of bar} = \frac{1563.27}{491} = 4$$

$$\text{Then we select 4 bars } \Phi 25 \quad A_{s_{\text{provided}}} = 4 * 491 = 1963.5 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c' * b * a$$

$$1963.5 * 420 = 0.85 * 30 * 800 * a$$

$$a = 40.42mm$$

$$\beta_1 = 0.85 - 0.007(fc - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{40.42}{0.836} = 48.36mm$$

$$\varepsilon_s = \frac{437.5 - 48.36}{48.36} \times 0.003$$

$$\varepsilon_s = 0.024 > 0.005$$

$$\Phi * Mn = \Phi * As * fy * (d - \frac{a}{2})$$

$$\Phi * Mn = 0.9 * 1963.5 * 420 * (437.5 - 20.21) = 309.71 > 249 \text{ singly reinforcement}$$

**Check for spacing between the bar**

$$S = \frac{800 - 2 * 40 - 2 * 10 - 4 * 25}{3}$$

$$S = 200mm \geq 25mm$$

**MAX. Negative Moment=216.5 KN.m**

$$bw = 80cm, h = 50cm$$

$$d = 437.5mm$$

$$Mu = 216.5 \text{ KN.m}$$

$$Mn = \frac{Mu}{\Phi} = \frac{216.5}{0.9} = 240.56 \text{ KN.m}$$

$$As_{min} = \frac{\sqrt{fc'}}{4(fy)} (bw)(d) \geq \frac{1.4}{fy} (bw)(d).$$

$$As_{min} = \frac{\sqrt{30}}{4(420)} (800)(437.5) \geq \frac{1.4}{420} (800)(437.5)$$

$$As_{min} = 1141.1mm^2 < 1166.7mm^2 \dots\dots\dots\text{the larger is control}$$

$$As_{min} = 1166.7mm^2$$

$$R_n = \frac{M_n}{b * d^2}$$

$$R_n = \frac{240.56}{800 * 437.5^2} = 1.57 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 * f_c} = \frac{420}{0.85 * 30} = 16.5$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right)$$

$$\rho = \frac{1}{16.5} \left( 1 - \sqrt{1 - \frac{2(16.5)(1.57)}{420}} \right) = 0.00386$$

$$A_{req} = \rho * b * d = 0.00386 * 800 * 437.5 = 1352.25 \text{ mm}^2$$

$$1352.25 \text{ mm}^2 > A_{s_{min}} = 1166.7 \text{ mm}^2$$

$$\text{Use } 3 \Phi 25 \gg \# \text{ of bar} = \frac{1352.25}{491} = 3$$

$$\text{Then we select 3 bars } \Phi 25 \quad A_{s_{provided}} = 3 * 491 = 1472.62 \text{ mm}^2$$

### Check for yielding

Tension = compression

$$A_s * f_y = 0.85 * f_c * b * a$$

$$1472.62 * 420 = 0.85 * 30 * 800 * a$$

$$a = 30.32 \text{ mm}$$

$$\beta_1 = 0.85 - 0.007(f_c - 28)$$

$$\beta_1 = 0.85 - 0.007(30 - 28) = 0.836$$

$$x = \frac{a}{\beta_1} = \frac{30.32}{0.836} = 36.27 \text{ mm}$$

$$\epsilon_s = \frac{437.5 - 36.27}{36.27} \times 0.003$$

$$\epsilon_s = 0.033 > 0.005$$

$$\Phi * M_n = \Phi * A_s * f_y * \left( d - \frac{a}{2} \right)$$

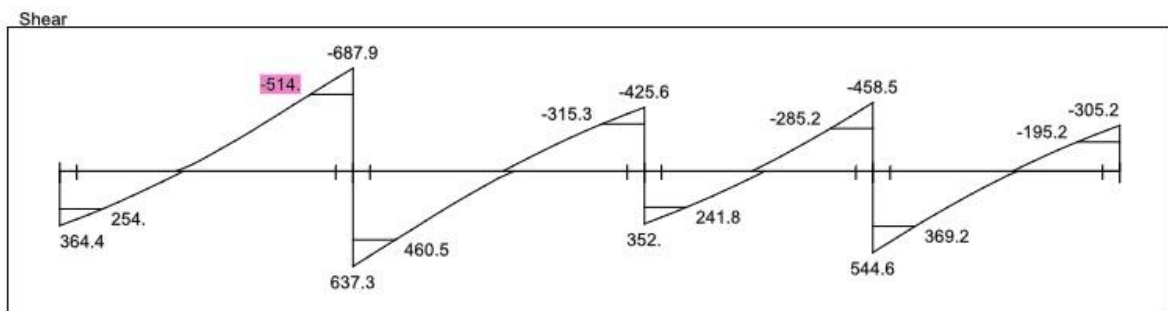
$$\Phi * M_n = 0.9 * 1472.62 * 420 * (437.5 - 15.16) = 235.095 > 216.5 \text{ singly reinforcement}$$

### Check for spacing between the bar

$$S = \frac{800 - 2 * 40 - 2 * 10 - 3 * 25}{2}$$

$$S = 312.5 \text{ mm} \geq 25 \text{ mm}$$

### ✓ Design of shear



Shear Envelope (factored) units:KN Fig(4-6)

$$V_{u,max} = 514 \text{ KN}$$

$$d = 500 - 40 - 10 - 12.5 = 437.5 \text{ mm}$$

$$V_c = \frac{\sqrt{f_c'}}{6} b_w * d$$

$$V_c = \frac{\sqrt{30}}{6} * 800 * 437.5 * 10^{-3} = 319.5 \text{ KN}$$

$$= 0.75 * 319.5 = 239.63 \text{ KN} < V_{u,max} = 514 \text{ KN}$$

$$\Phi V_{s,\min}=0.75 \left(\frac{1}{16}\right) \sqrt{f_c'} * b_w * d = 0.75 \left(\frac{1}{16}\right) \sqrt{30} * 800 * 437.5 = 89.9 \text{ kN} \quad \text{-control-}$$

$$\Phi V_{s,\min} = 0.75 \left(\frac{1}{3}\right) * b_w * d = 0.75 \left(\frac{1}{3}\right) * 800 * 437.5 = 87.5 \text{ kN}$$

$$\Phi V_c + \Phi V_{s,\min} = 329.53 \text{ kN} < V_{u,\max}$$

$$\Phi \tilde{V}_s = 0.75 \left(\frac{1}{3}\right) * b_w * d = 0.75 \left(\frac{1}{3}\right) * \sqrt{30} * 800 * 437.5 = 479.26 \text{ kN}$$

$$\Phi V_c + \Phi \tilde{V}_s = 239.63 + 479.26 = 718.89 \text{ kN} > V_{u,\max} = 514 \text{ kN}$$

-Stirrups are required-

Use 4 leg  $\phi 10$

$$A_v = 314.2 \text{ mm}^2$$

$$\tilde{V}_s = \frac{479.26}{0.75} = 639.01 \text{ kN}$$

$$\frac{A_v}{s} = \frac{V_s}{f_y * d}$$

$$S_{\text{req}} = \frac{314.2 * 420 * 437.5}{639.01 * 10^3} = 90.35 \text{ mm} < \frac{d}{2} = 218.75 \text{ mm},, S = 7.5 \text{ cm}$$

## 4.7 Design Two Way Ribbed Slab

### ✓ Determination of Thickness for Two Way Ribbed Slab:

Assume H = 35cm

$$I_{b1} = \frac{100 \cdot 35^3}{12} = 357291.66 \text{ cm}^4$$

$$I_{b2} = \frac{80 \cdot 35^3}{12} = 285833.3 \text{ cm}^4$$

$$I_{b3} = \frac{100 \cdot 35^3}{12} = 337291.66 \text{ cm}^4$$

$$I_{b4} = \frac{80 \cdot 35^3}{12} = 285833.3 \text{ cm}^4$$

$$Y_c = \frac{40 \cdot 8 \cdot 4 + 35 \cdot 12 \cdot 16}{40 \cdot 8 + 35 \cdot 12} = 10.81 \text{ cm}$$

$$I_r = \frac{52 \cdot 10.81^3}{3} - \frac{40 \cdot 2.81^3}{3} + \frac{21 \cdot 24.19^3}{3} = 78219.6 \text{ cm}^4$$

$$I_{s1} = \frac{78219.6 \cdot \left(\frac{600}{2} + 80\right)}{52} = 571604.77 \text{ cm}^4$$

$$I_{s2} = \frac{78219.6 \cdot \left(\frac{589}{2} + 80\right)}{52} = 563331.54 \text{ cm}^4$$

$$I_{s3} = \frac{78219.6 \cdot \left(\frac{600}{2} + 100\right)}{52} = 601689.23 \text{ cm}^4$$

$$I_{s4} = \frac{78219.6 \cdot \left(\frac{589}{2} + 100\right)}{52} = 593416 \text{ cm}^4$$

$$\alpha_1 = \frac{285833.3}{563331.54} = 0.51$$

$$\alpha_2 = \frac{357291.66}{601689.23} = 0.59$$

$$\alpha_3 = \frac{337291.66}{593416} = 0.57$$

$$\alpha_4 = \frac{285833.3}{601689.23} = 0.48$$

$$\alpha_{fm} = \frac{0.51+0.59+0.57+0.48}{4} = 0.538 > 0.2$$

$$\beta = \frac{6}{5.89} = 1.02$$

$$h_{min} = \frac{6000 * (0.8 + (\frac{420}{1400}))}{36 + 1.02 * 5 * (0.538 - 0.2)} = 174.9 \text{ mm}$$

$$h = 35 \text{ cm} > h_{min} = 17.49 \text{ cm}$$

#### ✓ Load Calculation:

Parts of Flight	Calculation
<b>Tiles</b>	<b><math>22 * 0.03 * 0.52 * 0.52 = 0.178 \text{ KN}</math></b>
<b>Mortar</b>	<b><math>22 * 0.02 * 0.52 * 0.52 = 0.119 \text{ KN}</math></b>
<b>Sand</b>	<b><math>16 * 0.07 * 0.52 * 0.52 = 0.303 \text{ KN}</math></b>
<b>Topping</b>	<b><math>25 * 0.08 * 0.52 * 0.52 = 0.541 \text{ KN}</math></b>
<b>Rib</b>	<b><math>25 * 0.27 * 0.12 * (0.52 + 0.4) = 0.745 \text{ KN}</math></b>
<b>Block</b>	<b><math>9 * 0.27 * 0.4 * 0.4 = 0.389 \text{ KN}</math></b>
<b>Plaster</b>	<b><math>22 * 0.02 * 0.52 * 0.52 = 0.119 \text{ KN}</math></b>
<b>Sum</b>	<b>2.80 KN</b>

**Table ( 4.3 ) : Dead load from two way ribbed slab**



### Dead Load of slab:

$$DL = \frac{2.80}{0.52 \times 0.52} = 10.36 \text{ KN/m}^2$$

$$W_D = 1.2 \times 10.36 = 12.432 \text{ KN/m}^2$$

$$LL = 3 \text{ KN/m}^2$$

$$W_L = 1.6 \times 3 = 4.8 \text{ KN/m}^2$$

$$W = 12.432 + 4.8 = 17.232 \text{ KN/m}^2$$

### ✓ Moments Calculations:

From tables use Case (9 ):

$$C_{a, \text{neg}} = 0.0626 \text{ , , } C_{b, \text{neg}} = 0.0314$$

$$M_{a, \text{neg}} = C_{a, \text{neg}} \times W_u \times (L_a)^2 = 0.0626 \times 17.232 \times (5.89)^2 \times 0.52 = 20.1 \text{ KN .m / rib.}$$

$$M_{b, \text{neg}} = C_{b, \text{neg}} \times W_u \times (L_b)^2 = 0.0314 \times 17.232 \times (6)^2 \times 0.52 = 10.13 \text{ KN .m / rib.}$$

$$C_{a, \text{dL}}^+ = 0.0234 \text{ , , } C_{b, \text{dL}}^+ = 0.019$$

$$M_{a, \text{d}}^+ = C_{a, \text{dL}}^+ \times W_{ud} \times (L_a)^2 = 0.0234 \times 12.432 \times (5.89)^2 \times 0.52 = 5.25 \text{ KN .m / rib.}$$

$$M_{b, \text{d}}^+ = C_{b, \text{dL}}^+ \times W_{ud} \times (L_b)^2 = 0.019 \times 12.432 \times (6)^2 \times 0.52 = 4.42 \text{ KN .m / rib.}$$

$$C_{a, \text{LL}}^+ = 0.031 \text{ , , } C_{b, \text{LL}}^+ = 0.027$$

$$M_{a, \text{L}}^+ = C_{a, \text{LL}}^+ \times W_{ul} \times (L_a)^2 = 0.031 \times 4.8 \times (5.89)^2 \times 0.52 = 2.68 \text{ KN .m / rib.}$$

$$M_{b,L}^+ = C_{b,LL} \times W_{ul} \times (L_b)^2 = 0.027 \times 4.8 \times (6)^2 \times 0.52 = 2.43 \text{ KN.m / rib.}$$

$$M_a \text{ positive} = 5.25 + 2.68 = 7.93 \text{ KN.m / rib.}$$

$$M_b \text{ positive} = 4.42 + 2.43 = 6.85 \text{ KN.m / rib.}$$

Negative moment at discontinuous edges = 1/3 positive.

$$M_b \text{ neg} = (1/3) \times 6.85 = 2.28 \text{ KN.m / rib.}$$

### ✓ Design of positive moments:

**Design of Positive Moment :- (Ma=7.39KN.m)**

Assume bar diameter  $\phi$  14 for main positive reinforcement

$$d = h - \text{cover} - d_{\text{stirrups}} - \frac{d_b}{2} = 350 - 20 - 8 - \frac{14}{2} = 315 \text{ mm}$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{7.39 \times 10^6}{0.9 \times 520 \times 315^2} = 0.16 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 \times 24} = 20.6$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2 \cdot m \cdot R_n}{420}} \right) = \frac{1}{20.6} \left( 1 - \sqrt{1 - \frac{2 \times 20.6 \times 0.16}{420}} \right) = 0.000382$$

$$A_{s, \text{req}} = \rho \cdot b \cdot d = 0.000382 \times 520 \times 315 = 62.65 \text{ mm}^2$$

**Check for As min:-**

$$A_{s \text{ min}} = \frac{\sqrt{f'_c}}{4(f_y)} (b_w)(d) \text{ **ACI-318 (10.5.1)}**$$

$$A_{s \text{ min}} = \frac{\sqrt{24}}{4(420)} (120)(315) = 110.22 \text{ mm}^2$$

$$A_s \min = \frac{1.4}{(f_y)} (bw)(d)$$

$$A_s \min = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \dots \text{controls}$$

$$A_{s, \text{req}} = 62.65 \text{ mm}^2 < A_{s, \min} = 126 \text{ mm}^2 \dots \text{OK}$$

**Use 2  $\phi 10$ ,  $A_s$ , provided = 157.08 mm<sup>2</sup> >  $A_{s, \text{required}}$  = 126 mm<sup>2</sup>... Ok**

**Check for strain:-**

$$a = \frac{A_s f_y}{0.85 b f'_c} = \frac{157.08 \times 420}{0.85 \times 520 \times 24} = 6.22 \text{ mm}$$

$$x = \frac{a}{\beta_1} = \frac{6.22}{0.85} = 7.32 \text{ mm}$$

$$\varepsilon_s = 0.003 \left( \frac{d - x}{x} \right) = 0.003 \left( \frac{315 - 7.32}{7.32} \right) = 0.126 > 0.005 \quad \text{Ok}$$

**Design of Positive Moment:- ( $M_b = 6.85 \text{ kN.m}$ )**

$$d = h - \text{cover} - d_{\text{stirrups}} - \frac{d_b}{2} = 350 - 20 - 8 - \frac{14}{2} = 315 \text{ mm}$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{6.85 \times 10^6}{0.9 \times 520 \times 315^2} = 0.148 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 \times 24} = 20.6$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2 m R_n}{420}} \right) = \frac{1}{20.6} \left( 1 - \sqrt{1 - \frac{2 \times 20.6 \times 0.148}{420}} \right) = 0.000354$$

$$A_{s, \text{req}} = \rho \cdot b \cdot d = 0.000354 \times 520 \times 315 = 57.99 \text{ mm}^2$$

**Check for As min:-**

$$A_{s \min} = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \text{ **ACI-318 (10.5.1)**}$$

$$A_{s \min} = \frac{\sqrt{24}}{4(420)} (120)(315) = 110.22 \text{ mm}^2$$

$$A_{s \min} = \frac{1.4}{(f_y)} (b_w)(d)$$

$$A_{s \min} = \frac{1.4}{420} (120)(315) = 126 \text{ mm}^2 \text{ .....controls}$$

$$A_{s_{\text{req}}} = 57.99 \text{ mm}^2 < A_{s_{\text{min}}} = 126 \text{ mm}^2 \text{ .....OK}$$

**Use 2  $\phi 10$ , As, provided= 157.08 mm<sup>2</sup> > A<sub>s, required</sub>= 126 mm<sup>2</sup>... Ok**

**Check for strain:-**

$$a = \frac{A_s f_y}{0.85 b f_c'} = \frac{157.08 \times 420}{0.85 \times 520 \times 24} = 6.22 \text{ mm}$$

$$x = \frac{a}{\beta_1} = \frac{6.22}{0.85} = 7.32 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d - x}{x} \right) = 0.003 \left( \frac{315 - 7.32}{7.32} \right) = 0.126 > 0.005 \quad \text{Ok}$$

✓ **Design of negative moments:**

**Design of Negative Moment :- (Ma=-20.1KN.m)**

Assume bar diameter  $\phi 12$  for negative reinforcement

$$d = h - \text{cover} - d_{\text{stirrups}} - \frac{d_b}{2} = 350 - 20 - 8 - \frac{12}{2} = 316 \text{ mm}$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{20.1 \times 10^6}{0.9 \times 120 \times 316^2} = 1.86 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 f'_c} = \frac{420}{0.85 \times 24} = 20.6$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2 m R_n}{420}} \right) = \frac{1}{20.6} \left( 1 - \sqrt{1 - \frac{2 \times 20.6 \times 1.86}{420}} \right) = 0.0047$$

$$A_{s, \text{req}} = \rho \cdot b \cdot d = 0.0047 \times 120 \times 316 = 178.22 \text{ mm}^2$$

**Check for As min:-**

$$A_{s \text{ min}} = \frac{\sqrt{f'_c}}{4(f_y)} (b_w)(d) \text{ **ACI-318 (10.5.1)}**$$

$$A_{s \text{ min}} = \frac{\sqrt{24}}{4(420)} (120)(316) = 110.5 \text{ mm}^2$$

$$A_{s \text{ min}} = \frac{1.4}{(f_y)} (b_w)(d)$$

$$A_{s \text{ min}} = \frac{1.4}{420} (120)(316) = 126.4 \text{ mm}^2 \text{ ....controls}$$

$$A_{s, \text{req}} = 178.22 > A_{s, \text{min}} = 126.4 \text{ mm}^2 \text{ ....OK}$$

**Use 2 ø12,  $A_{s, \text{provided}} = 226.2 \text{ mm}^2 > A_{s, \text{required}} = 178.22 \text{ mm}^2$ ... Ok**

**Check for strain:-**

$$a = \frac{A_s f_y}{0.85 b f'_c} = \frac{226.2 \times 420}{0.85 \times 120 \times 24} = 38.81 \text{ mm}$$

$$x = \frac{a}{\beta_1} = \frac{38.81}{0.85} = 45.66 \text{ mm}$$

$$\epsilon_s = 0.003 \left( \frac{d - x}{x} \right) = 0.003 \left( \frac{316 - 45.66}{45.66} \right) = 0.0178 > 0.005 \quad \text{Ok}$$

✓ Design of Negative Moment :-

(Mb=-10.13KN.m)

Assume bar diameter  $\phi$  12 for negative reinforcement

$$d = h - \text{cover} - d_{\text{stirrups}} - \frac{d_b}{2} = 350 - 20 - 8 - \frac{12}{2} = 316 \text{ mm}$$

$$R_n = \frac{M_u}{\phi b d^2} = \frac{10.13 \times 10^6}{0.9 \times 120 \times 316^2} = 0.94 \text{ Mpa}$$

$$m = \frac{f_y}{0.85 f_c'} = \frac{420}{0.85 \times 24} = 20.6$$

$$\rho = \frac{1}{m} \left( 1 - \sqrt{1 - \frac{2 m R_n}{420}} \right) = \frac{1}{20.6} \left( 1 - \sqrt{1 - \frac{2 \times 20.6 \times 0.94}{420}} \right) = 0.00229$$

$$A_{s, \text{req}} = \rho \cdot b \cdot d = 0.00229 \times 120 \times 316 = 86.92 \text{ mm}^2$$

**Check for As min:-**

$$A_{s \text{ min}} = \frac{\sqrt{f_c'}}{4(f_y)} (b_w)(d) \text{ **ACI-318 (10.5.1)}**$$

$$A_{s \text{ min}} = \frac{\sqrt{24}}{4(420)} (120)(316) = 110.57 \text{ mm}^2$$

$$A_{s \text{ min}} = \frac{1.4}{(f_y)} (b_w)(d)$$

$$A_{s \text{ min}} = \frac{1.4}{420} (120)(316) = 126.4 \text{ mm}^2 \text{ ....controls}$$

$$A_{s, \text{req}} = 86.92 < A_{s, \text{min}} = 126.4 \text{ mm}^2 \text{ .....OK}$$

**Use 2  $\phi$ 12,  $A_{s, \text{provided}} = 226.2 \text{ mm}^2 > A_{s, \text{required}} = 126.4 \text{ mm}^2 \text{ ... Ok}$**

**Check for strain:-**

$$a = \frac{A_s f_y}{0.85 b f_c} = \frac{226.2 \times 420}{0.85 \times 120 \times 24} = 38.81 \text{ mm}$$

$$x = \frac{a}{\beta_1} = \frac{38.81}{0.85} = 45.66 \text{ mm}$$

$$\varepsilon_s = 0.003 \left( \frac{d - x}{x} \right) = 0.003 \left( \frac{316 - 45.66}{45.66} \right) = 0.0178 > 0.005 \quad \text{Ok}$$

✓ Design of shear for rib:

Maximum shear coefficient in short direction as in case (9)  $W_a @ m = 0.98$

$$W_a = 0.686$$

The total load on the panel  $= 5.89 \times 6 \times 17.232 = 608.98 \text{ KN}$

The load per rib at the face of long beam  $= 0.686 \times 608.98 \times 0.52 / (2 \times 6) = 18.1 \text{ KN}$

$$W_b = 0.306$$

The total load on the panel  $= 5.89 \times 6 \times 17.232 = 608.98 \text{ KN}$

The load / rib at the face of long beam  $= 0.306 \times 608.98 \times 0.52 / (2 \times 5.89) = 8.23 \text{ KN}$

$$V_{ud} = V_{uface} - W_u \times b_f \times d = 18.1 - 17.232 \times 0.52 \times 0.316 = 15.27 \text{ KN}$$

**The shear strength of one rib:**

$$V_c = \frac{1.1}{6} \sqrt{f_c'} b_w d = \frac{1.1}{6} \sqrt{24} \times 120 \times 316 \times 10^{-3} = 34.05 \text{ KN}$$

$$\phi V_c = 0.75 \times 34.05 = 25.54 \text{ KN}$$

$$0.5 \phi V_c = 0.5 \times 25.54 = 12.77 \text{ KN}$$

$$0.5 \phi V_c < V_{ud} < \phi V_c$$

$$12.77 < 15.27 < 25.54$$

Minimum shear reinforcement is required except for joist construction.

$$V_{ud} = 17.232 * 0.52 * (3.8 - 0.316) = 31.3 \text{ KN}$$

$$\phi V_c = 25.54 < V_{ud} = 31.3 \text{ KN}$$

$$\phi V_{smin} \geq 0.75 \left( \frac{1}{3} \right) * b_w * d = 0.75 * \left( \frac{1}{3} \right) * 120 * 316 * 10^{-3} = 9.48 \text{ KN} \dots \text{Controls}$$

$$\phi V_{smin} \geq 0.75 \left( \frac{\sqrt{f_c'}}{16} \right) * b_w * d = 0.75 * \left( \frac{\sqrt{24}}{16} \right) * 120 * 316 * 10^{-3} = 8.7 \text{ KN}$$

$$\phi (V_c + V_{smin}) = 35.021 > V_u = 31.3 > \phi V_c = 25.54$$

$$V_s' = \frac{1}{3} \sqrt{f_c'} * b_w * d = 61.9 \text{ KN}$$

$$V_s = \frac{V_u}{\phi} - V_c = 12.92 \text{ KN}$$

$$V_{smin} = 11.4 < V_s = 12.92 < V_s' = 55.85 \dots \dots \text{Case IV}$$

Use 2 leg  $\Phi 8$

$$A_{vmin} = 100 \text{ mm}^2$$

$$\frac{A_{vmin}}{s} = \frac{v_s}{df_{yt}}$$

$$s = \frac{A_{vmin}}{v_s} df_{yt}$$

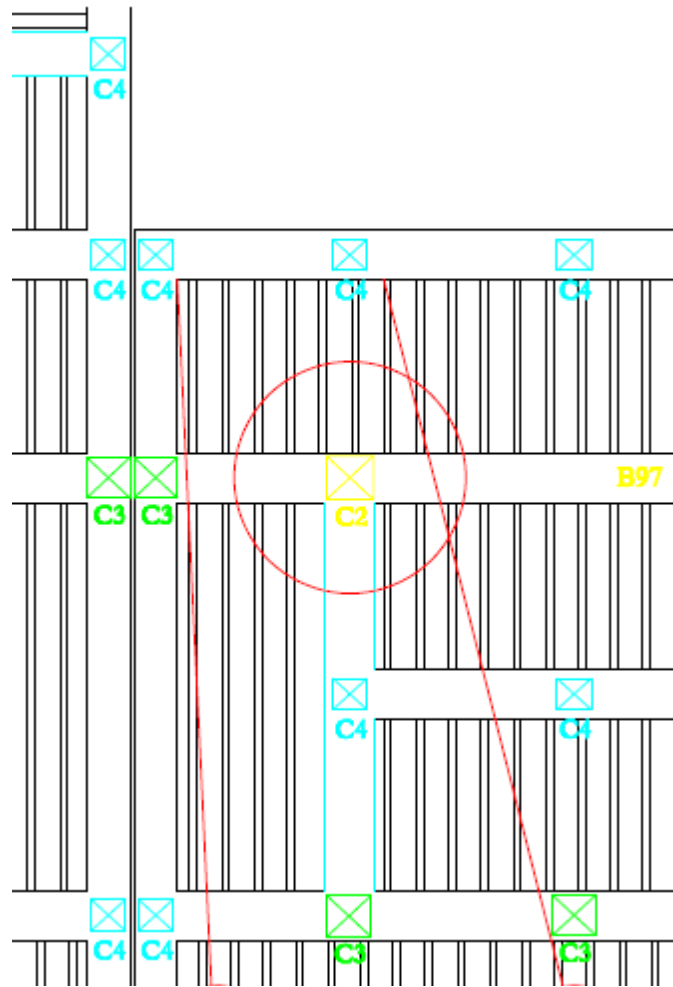
$$S = 926.5 \text{ mm}$$

$$s_{max} \leq \frac{d}{2} = \frac{285}{2} = 142.5 \text{ mm} \quad \text{or } s_{max} \leq 600 \text{ mm}$$

Use 4 leg  $\Phi 8 @ 125 \text{ mm}$



#### 4.7 Design of column (C36)



**Fig.(37) :Place Of Column (C36) within the second basement floor.**

#### **Load Calculation for Column**

Column	Column Dimensions	$f_c'$	$f_y$
Col. C36	60cm* 45cm	24Mpa	420Mpa

✓ **Load Calculation:**

$$P_u = 1941.6 \text{ KN}$$

$$\text{Use } \rightarrow \rho_g = \rho_g = 2\%$$

$$P_u = 0.65 * 0.8 * \{0.85 * f_c' (A_g - A_{st}) + A_{st} (f_y)\}$$

$$1941.6 * 10^3 = 0.65 * 0.8 * [0.85 * 24 * (A_g - 0.02 A_g) + 0.02 A_g * 420]$$

$$A_g = 133389.76 \text{ mm}^2$$

$$A_g = 600 * a$$

$$133389.76 / 600 = a$$

$$a = 222.3 \text{ mm}$$

Use  $600 \times 250 \text{ mm}$  with  $A_g = 150000 \text{ mm}^2$

<b>Pu(KN)</b>	<b><math>\rho_g</math></b>	<b><math>A_g, \text{provided}</math></b>	<b>a( mm )</b>	<b><math>A_g, \text{required}</math></b>
1941.6	0.02	$150000 \text{ mm}^2$	222.3	$133389.76 \text{ mm}^2$

✓ **Selecting longitudinal bars:**

$$P_u = 0.65 * 0.8 * \{0.85 * f_c' (A_g - A_{st}) + A_{st} (f_y)\}$$

$$1941.6 * 10^3 = 0.65 * 0.8 * [0.85 * 24 * (150000 - A_{st}) + A_{st} * 400]$$

$$A_{st} = 8737.6 \text{ mm}^2$$

**Take  $18\Phi 25$  As,provided =  $8834.4 \text{ mm}^2 > A_{s,req} = 8737.6 \text{ mm}^2$**

$$\rho_g = \frac{A_{st}}{A_g} = \frac{8834.4}{150000} = 0.017$$

<b><math>\Phi</math></b>	<b><math>A_{st, \text{required}}</math></b>	<b><math>\rho_g</math></b>
0.65	$8737.6 \text{ mm}^2$	0.017

✓ **Design of Ties:**

- Use ties  $\Phi 10$  with spacing of ties shall not exceed the smallest of

1.  $48 * d_s = 48 * 10 = 480\text{mm}$
2.  $16 * d_b = 16 * 25 = 400 \text{ mm}$  - control
3. the least dimension of the column = 700 mm

**Use ties  $\Phi 10$  @ 200mm**

ds(mm)	db(mm)	S(mm)
$\Phi 10$	$\Phi 25$	200

✓ **Check for code requirements:**

$$1. \quad \text{Clear Spacing} = \frac{750 - 40 * 2 - 10 * 2 - 6 * 25}{5} = 100 \text{ mm} >$$

$$40\text{mm} > 1.5d_b = 1.5 * 25 = 37.5\text{mm} - \text{OK}$$

$$2. \quad 0.01 < \rho_g = 0.017 < 0.08 - \text{OK}$$

$$3. \quad \text{Number of bars } 18 > 4 \text{ for rectangular section} - \text{OK}$$

$$4. \quad \text{Minimum tie diameter } d_s = \Phi 10 \text{ for } d_b = \Phi 25 \text{ bars} - \text{OK}$$

$$5. \quad \text{Arrangement of ties } 100 \text{ mm} < 150\text{mm} - \text{OK}$$

Clear Spacing	No. of bars	$\rho_g$	ds (mm)	db (mm)
100 mm	18	0.017	$\Phi 10$	$\Phi 25$

✓ **Check Slenderness Effect:**

$$\frac{klu}{r} < 34 - 12 \frac{M1}{M2} \quad \text{.....ACI - (10.12.2)}$$

Lu: Actual unsupported (un braced) length.

K: effective length factor (K= 1 for braced frame).

$$R: \text{radius of gyration} = 0.3 h = \sqrt{\frac{I}{A}}$$

$$Lu = 3.5 \text{ m}$$

$$M1/M2 = 1 \quad (\text{Braced frame with } M, \text{min})$$

**K=1** , According to ACI 318-02 The effective length factor, k, shall be permitted to be taken as 1.0.

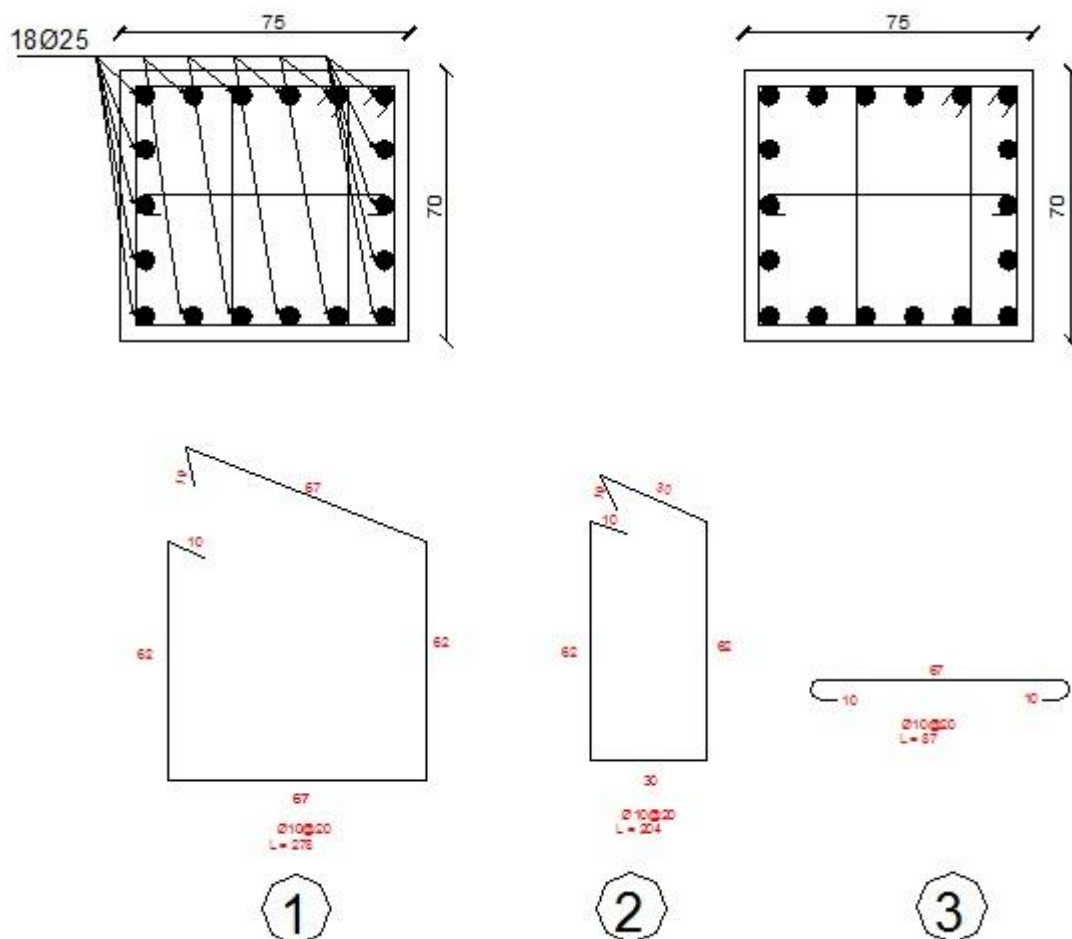
$$\frac{kl_u}{r} < 34 - 12 \frac{M_1}{M_2} = 22 < 40 \quad \dots\dots\dots \text{ACI} - (10.12.2)$$

$$\frac{kl_u}{r} = \frac{1 * 3.5}{0.3 * 0.750} = 15.55 < 22 < 40 \dots\dots$$

.....short column.

### Short column in both direction

Lu (m)	M1/M2	K	$\frac{kl_u}{r}$
3.5	1.0	1.0	15.55



**Fig. (38):Section of Column (C2)**







